

Hard and soft responses from parton transport

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**Workshop on Jet Quenching at RHIC vs LHC
in Light of Recent dAu vs pPb controls**

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in collaboration with Deke Sun

(parton) transport can give you:

- **bulk medium evolution**
- **nonequilibrium effects**
- **fluctuations**

Covariant transport

(on-shell) phase-space density $f(x, \vec{p}) \equiv \frac{dN(\vec{x}, \vec{p}, t)}{d^3x d^3p}$

transport equation:

$$p^\mu \partial_\mu f_i(x, p) = C_{2 \rightarrow 2}^i[\{f_j\}](x, p) + C_{2 \leftrightarrow 3}^i[\{f_j\}](x, p) + \dots$$

with, e.g.,

$$C_{2 \rightarrow 2}^i = \frac{1}{2} \sum_{jkl} \int_{234} (f_3^k f_4^l - f_1^i f_2^j) W_{12 \rightarrow 34}^{ij \rightarrow kl} \left(\int_j \equiv \int \frac{d^3 p_j}{2E_j}, \quad f_a^k \equiv f^k(x, p_a) \right)$$

fully causal and stable, can handle large gradients

near hydrodynamic limit, transport coefficients and relaxation times:

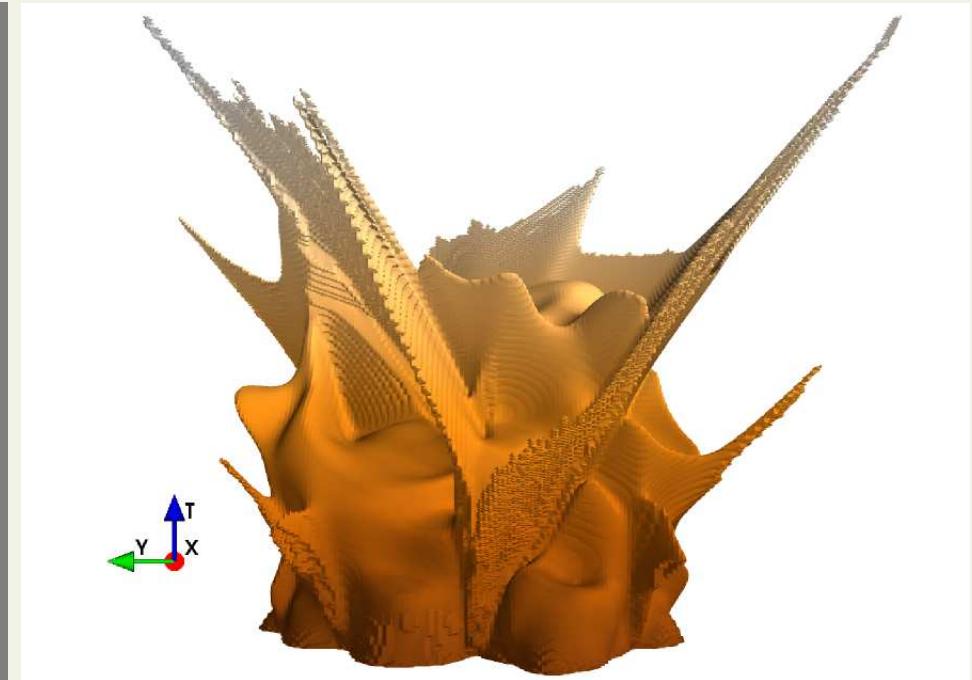
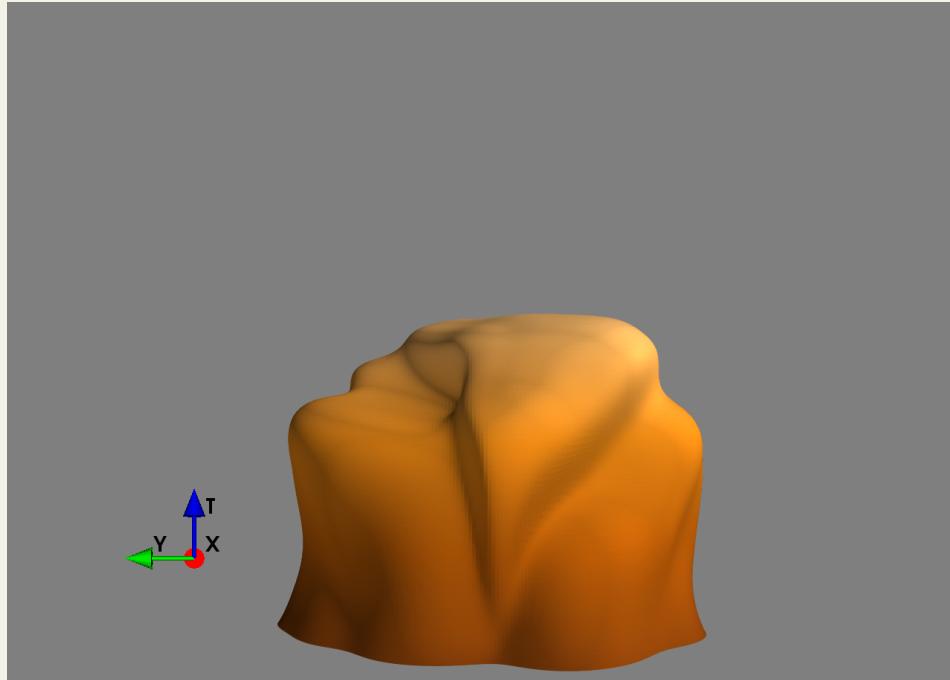
$$\eta \approx 1.2T/\sigma_{tr}, \quad \tau_\pi \approx 1.2\lambda_{tr}$$

Freezeout

Cooper-Frye: assumed sudden transition to a gas on a 3D hypersurface

$$E dN = p^\mu d\sigma_\mu(x) d^3p f_{gas}(x, \vec{p})$$

Huovinen & Holopainen (QM2012): $T_{FO} = \text{const}$ vs $\tau_{scatt}/\tau_{exp} = \text{const} ?!$

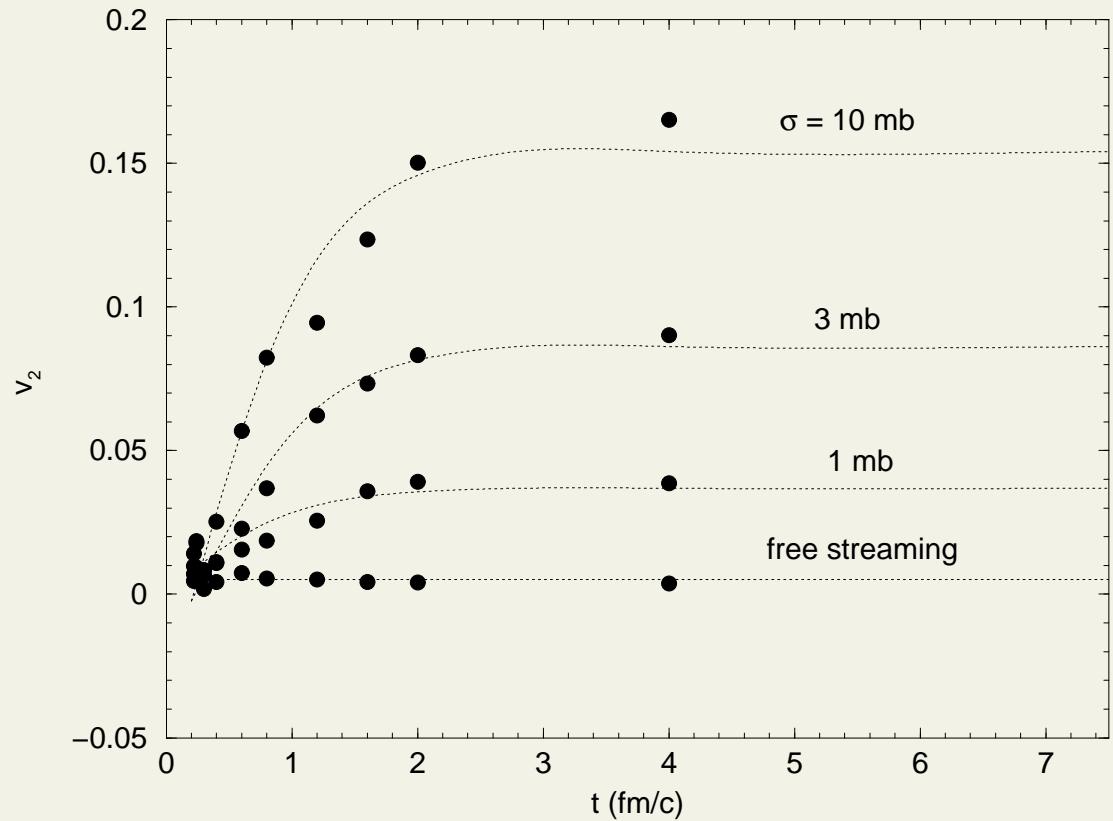


also need viscous corrections $f_{gas} = f_{equil} + \delta f$ (e.g., Wolff & Molnar @ QM2012)

Collectivity with suitable rates

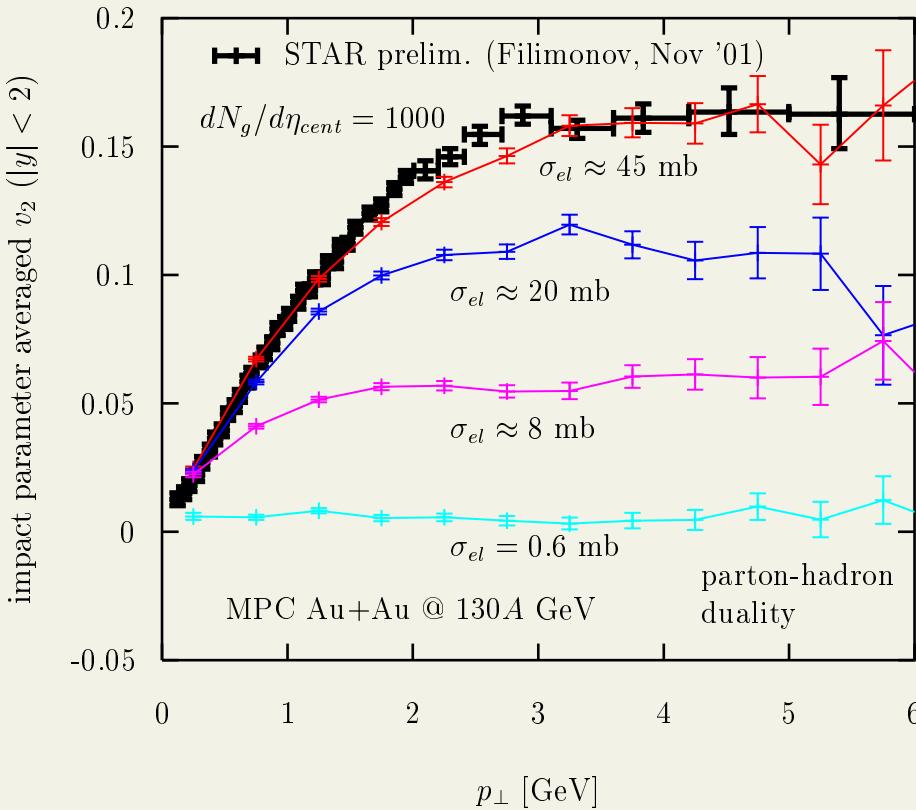
Zhang, Gyulassy & Ko ('99):

$2 \rightarrow 2$ transport ZPC

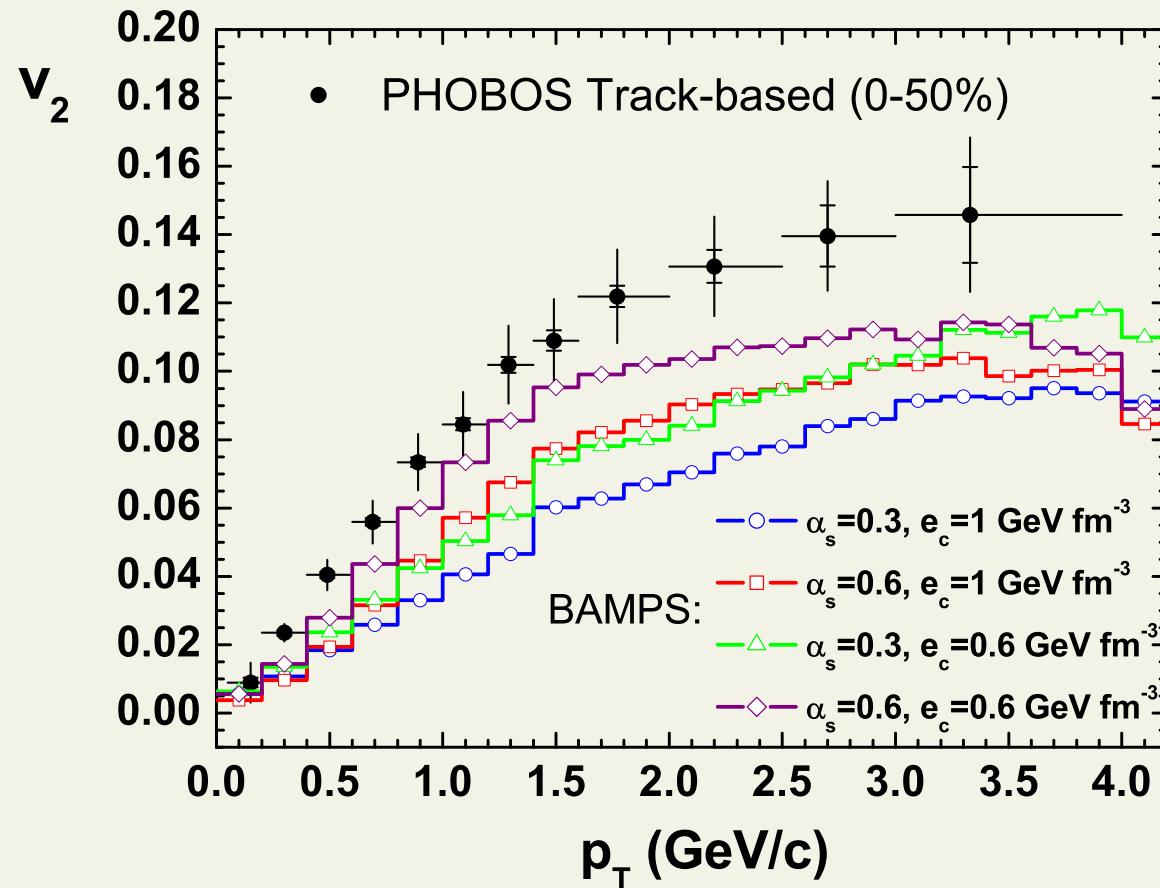


DM & Gyulassy, NPA 697 ('02):

$2 \rightarrow 2$ transport MPC



Xu & Greiner, ('08) **BAMPS claim: perturbative $3 \leftrightarrow 2$ rates thermalize**



Still to be confirmed...

matrix elements?

Application: bulk medium for jet quenching

E.g., line integrals

$$\Delta E_{GLV}^{(1)} \approx \frac{9\pi C_R \alpha_s^3}{4} \int d\tau \tau \rho(z_0 + v\tau, \tau) \ln \frac{2E}{\mu^2 \tau}$$

Gyulassy, Vitev, et al...

$$\frac{dE}{dL} = \kappa[s(L)]s(L)L$$

Shuryak & Liao

$$\frac{dE}{dL} = \text{const} \times E^\alpha L^\beta T^{2-\alpha+\beta}(L)$$

Betz et al

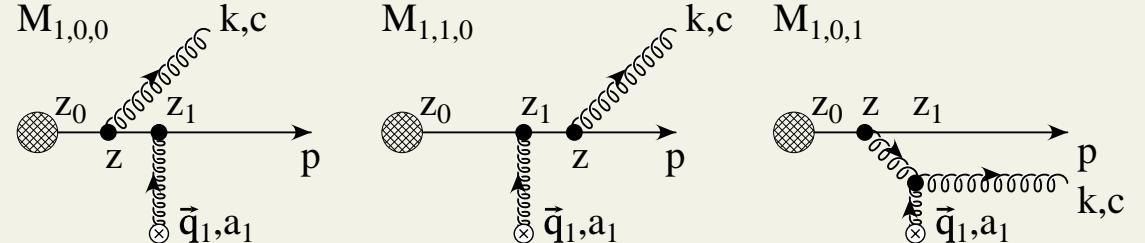
or stochastic E-loss

ΔE depends on the medium. E.g, GLV needs scattering center information

→ natural to combine (D)GLV with a parton transport model (MPC)

GLV - opacity expansion

Gyulassy, Levai, Vitev NPB594 ('00)



$$\begin{aligned}
 x \frac{dN^{(n)}}{dx d^2\mathbf{k}} = & \frac{C_R \alpha_s}{\pi^2} \frac{\chi^n}{n!} \int \prod_{i=1}^n \left\{ d\mathbf{q}_i \left(\frac{dz_i \rho_i \sigma_i}{\chi} \right) (\bar{v}_i^2(\mathbf{q}_i) - \delta^2(\mathbf{q}_i)) \right\} \\
 & \times \left[-2 \mathbf{C}_{(1,\dots,n)} \cdot \sum_{m=1}^n \mathbf{B}_{(m+1,\dots,n)(m,\dots,n)} \right. \\
 & \left. \left(\cos \left(\sum_{k=2}^m \omega_{(k,\dots,n)} \Delta z_k \right) - \cos \left(\sum_{k=1}^m \omega_{(k,\dots,n)} \Delta z_k \right) \right) \right]
 \end{aligned}$$

formation time $\omega_{n\dots m} = \frac{2xE}{(\mathbf{k}-\mathbf{q}_n-\dots-\mathbf{q}_m)^2}$

key assumptions: static Yukawa scatterers, soft emission, $\lambda_{MFP} \gg 1/\mu_D$

as usual, in the end interpret $\rho_i(\vec{x}) \rightarrow \rho_i(\vec{x}, t)$ along jet trajectory

Setup:

- Bulk dynamics evolution computed from covariant transport (MPC code)
DM & Gyulassy, PRC62 ('00)
- Here: only use the density $\rho(x_\perp, \tau)$
 - in principle, we could use spacetime location of scatterers for external jets embedded in transport (no jet recoil, forward scattering)
- Keep energy loss stochastic (no averaging over scattering location)
- Radiated glue considered “lost” and feedback on medium ignored - focus on high p_T

After E-loss, fragment as in vacuum (LO pQCD) to get some hadronic observables: R_{AA} and v_2

Medium evolution from kinetic theory (MPC transport code):

- $2 \rightarrow 2$ with massless gluons
- opacity set to generate sufficient $v_2(p_T) \sim 0.2$ at RHIC / LHC
- $\eta/s \approx 0.1$ dynamics via $\sigma_{gg} \sim 1/T^2 \sim \tau^{2/3}$ DM, arXiv:0806.0026
- boost-invariant initial conditions in $|\eta| < 5$ window

- LO pQCD jet production & fragmentation (CTEQ5L, BKK95, $K_{NLO} \approx 2.5$)
- jet and bulk transverse profiles $\propto \rho^{binary}(x_\perp)$, with $dN^{bulk}/dy \propto N_{part}$
- T set by $\rho(T)$ for massless gluon gas, $\mu_D = gT$
- $\tau_0 = 0.6$ fm formation, and LINEAR density buildup $\rho(\tau) \propto \tau$ for $\tau < \tau_0$

Two centralities: 0 – 10% ($b \approx 3$ fm) and 25 – 35% ($b \approx 8$ fm)

4 scenarios:

1D = longitudinal Bjorken expansion, $\langle \Delta E \rangle$

1D, stochastic = longitudinal Bjorken expansion, $\Delta E(z)$

3D = Bjorken AND transverse expansion, $\langle \Delta E \rangle$

3D, stochastic = Bjorken AND transverse expansion, $\Delta E(z)$

not the most sophisticated E-loss treatment

but we did include transverse expansion (unlike Buzzatti et al, Horowitz et al, Betz et al)

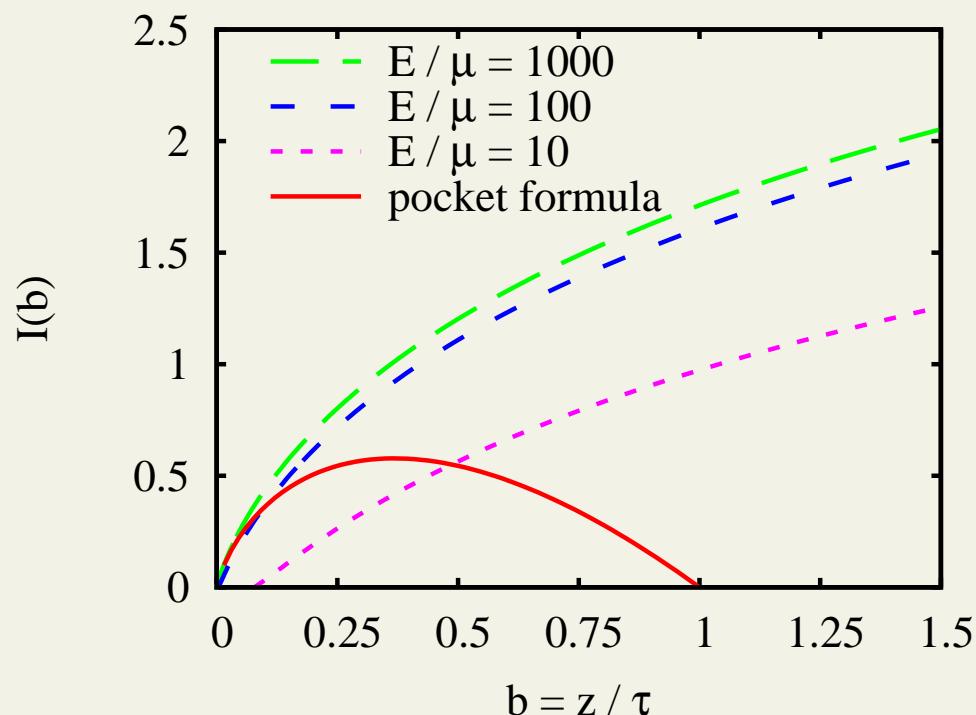
Finite energy & kinematics crucial:

$$|k| < \sim xE$$

$$|q| < \sim \sqrt{s} \sim \sqrt{6ET}$$

$$xE > \sim \mu \quad (\textbf{plasma})$$

$$\begin{aligned} \Delta E_{GLV}^{(1)}(z) &= \frac{C_R \alpha_s}{\pi^2} \chi \int dx dk dq \frac{\mu^2}{\pi(q^2 + \mu^2)^2} \frac{2k \cdot q}{k^2(k - q)^2} (1 - \cos \omega \Delta z) \\ &\equiv \frac{2C_R \alpha_s}{\pi} E \chi I(\Delta z / \tau(z), E / \mu(z)) \quad , \quad \omega \equiv (k - q)^2 / (2Ex) \end{aligned}$$



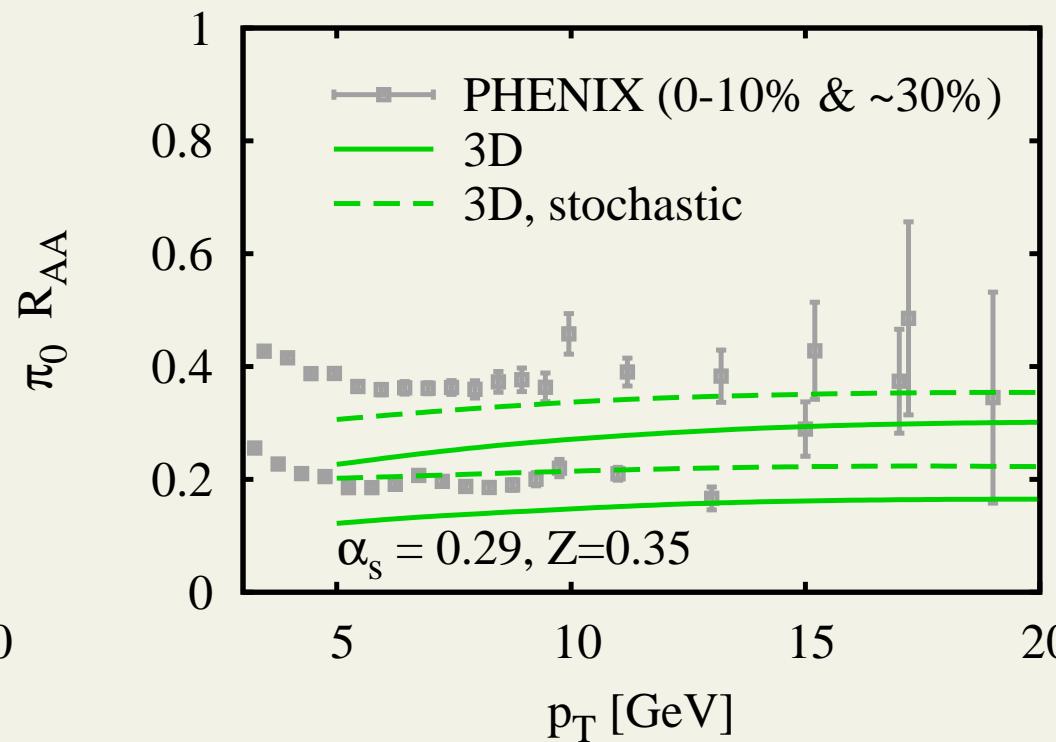
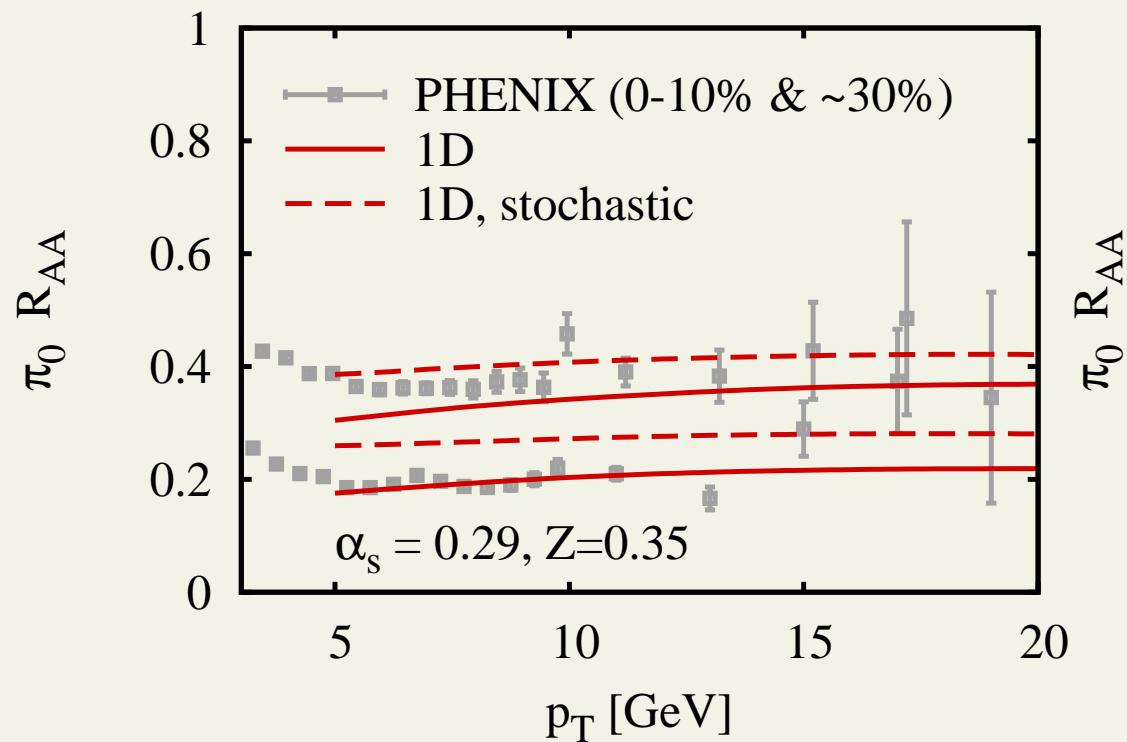
$$\tau(z) \equiv \frac{2E}{\mu^2(z)}$$

“pocket formula”

$$\langle \Delta E_{GLV}^{(1)} \rangle \sim \int \rho(z_0 + v\tau, \tau) \ln \frac{2E}{\mu^2 \tau}$$

not reliable

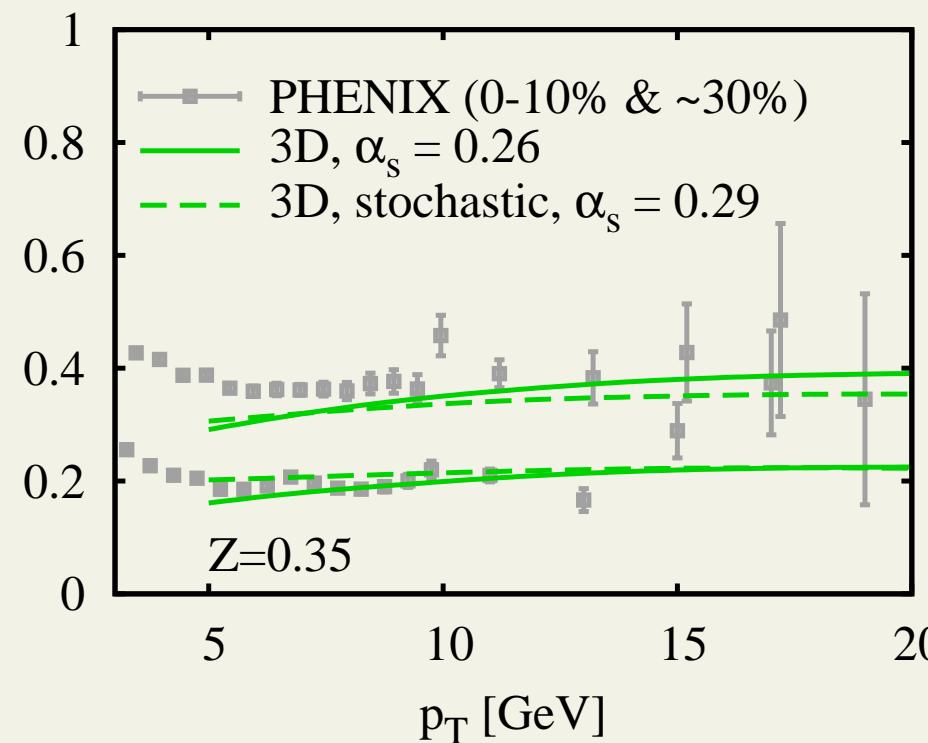
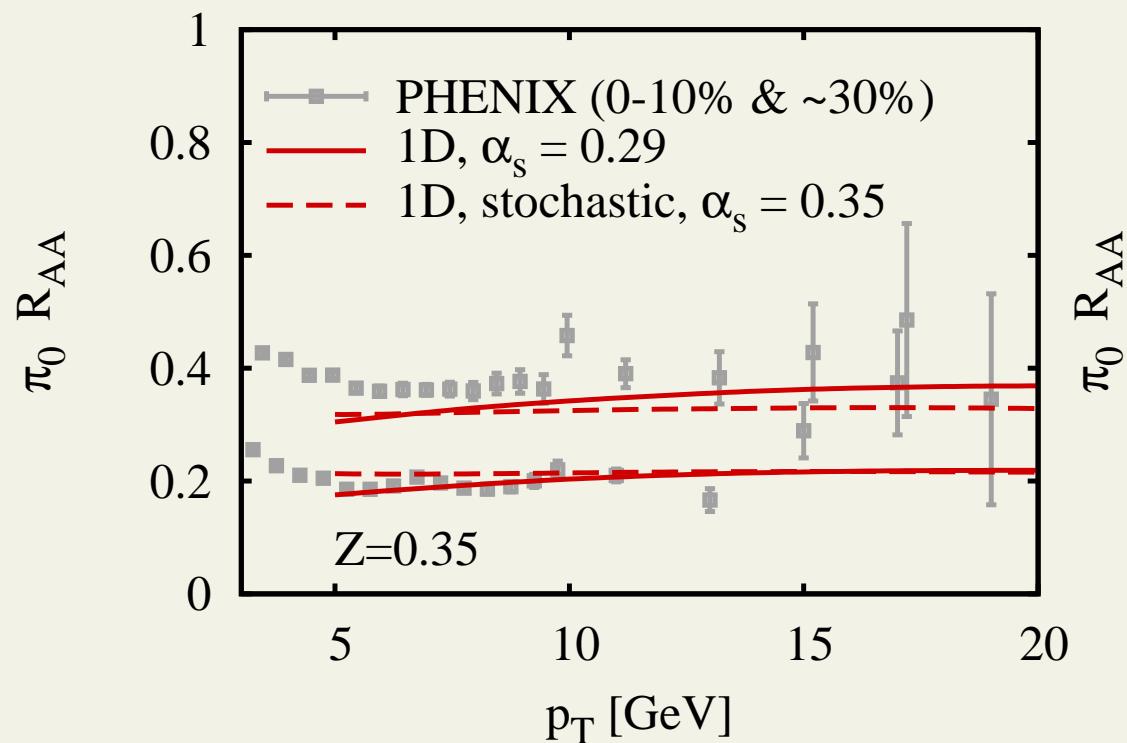
pion RAA, RHIC



fluctuations and transverse expansion matter

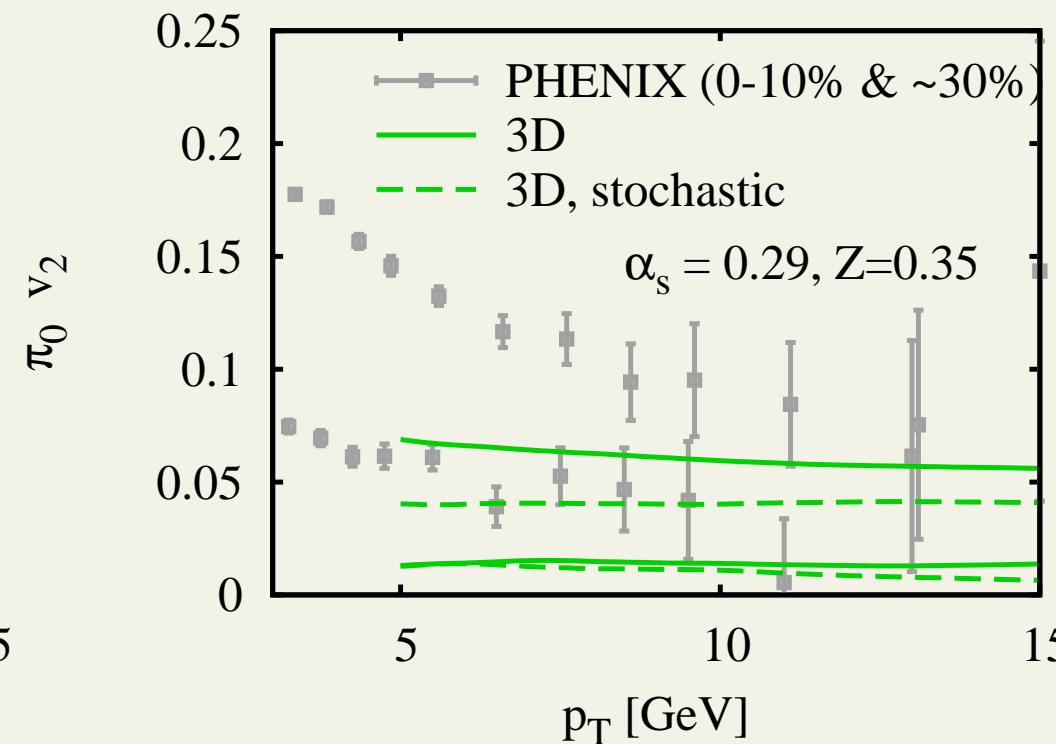
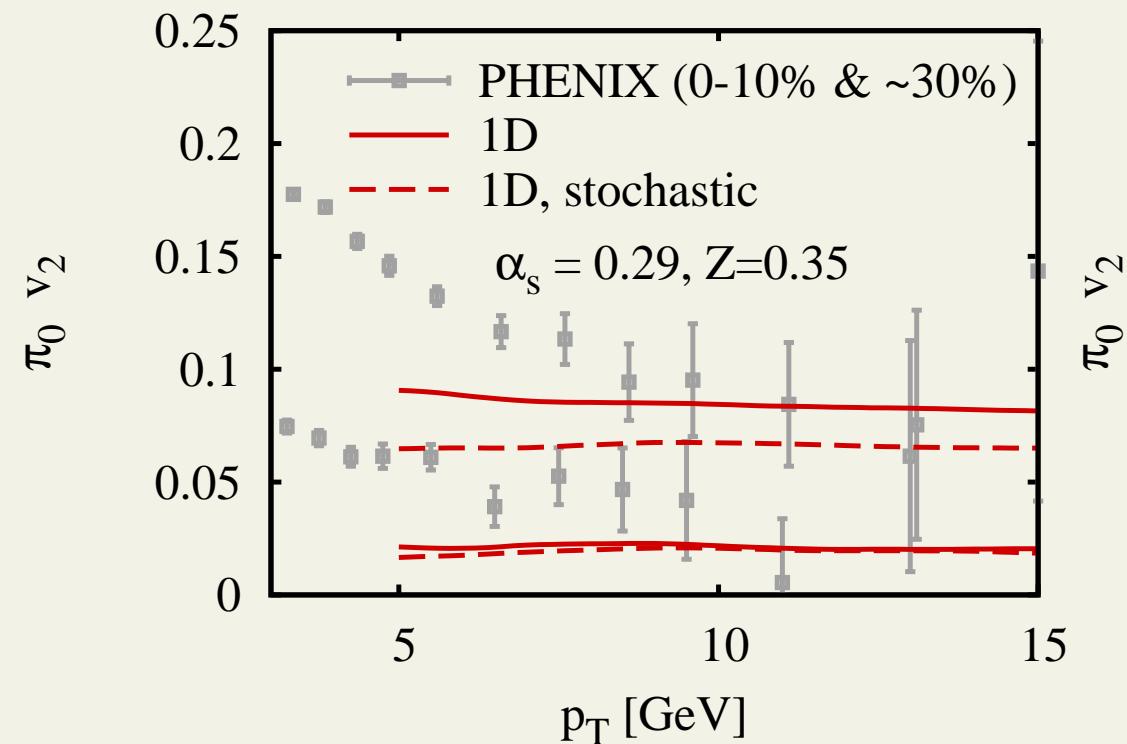
more energy loss with transverse expansion because GLV favors large $\Delta z/\tau_f$

pion RAA, RHIC - α_s scaled to RAA for central

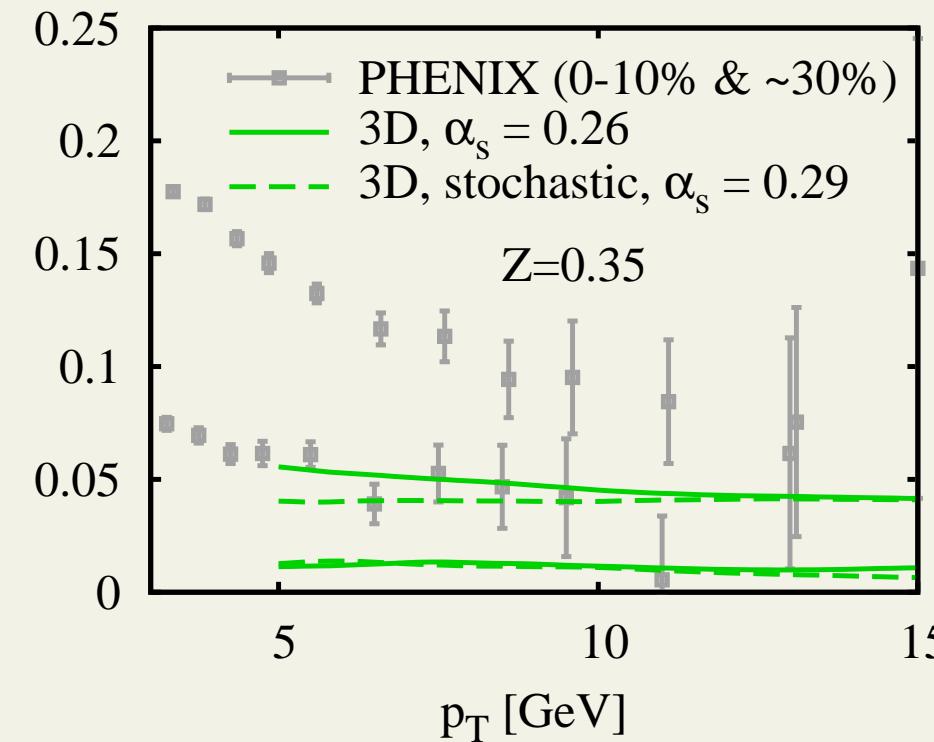
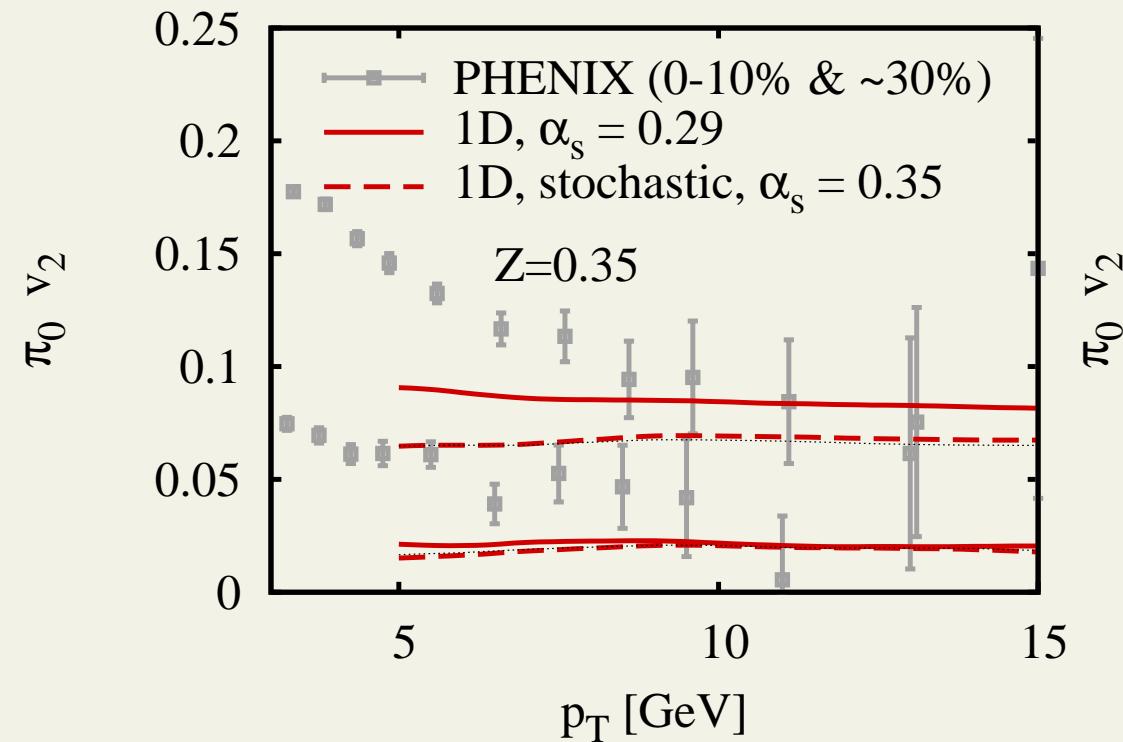


only small 10-15% differences after tuning parameters to central data

pion v_2 , RHIC



pion v_2 , RHIC - α_s scaled to RAA for central



challenging to get enough $v_2 > 4 - 5\%$ with expanding medium

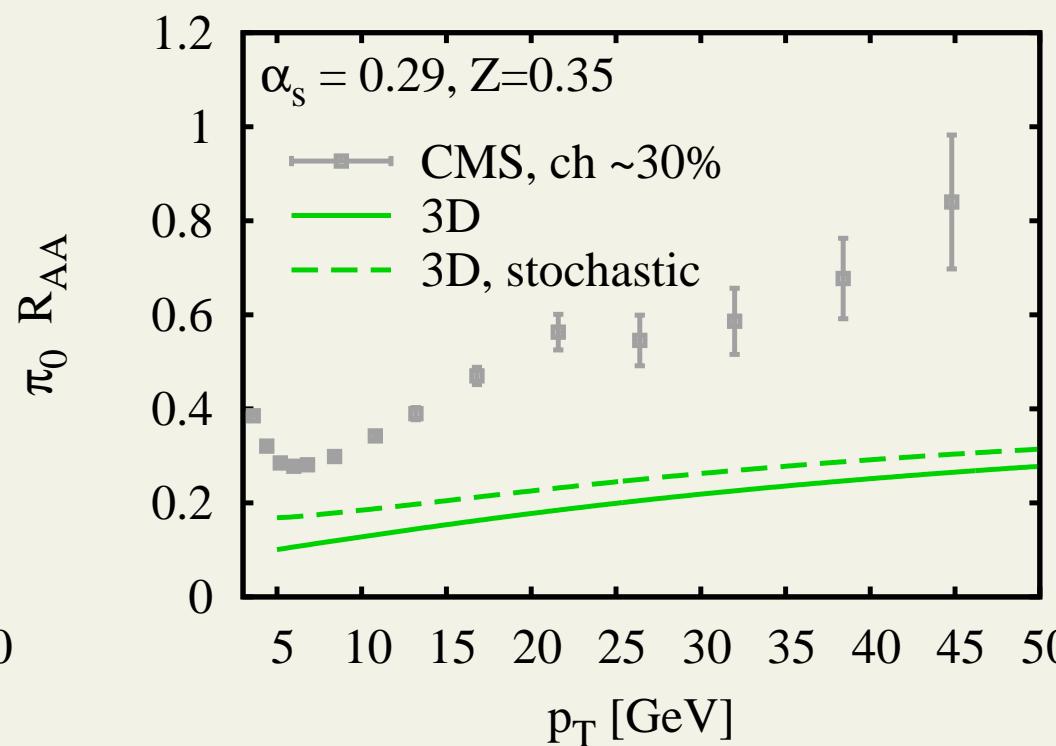
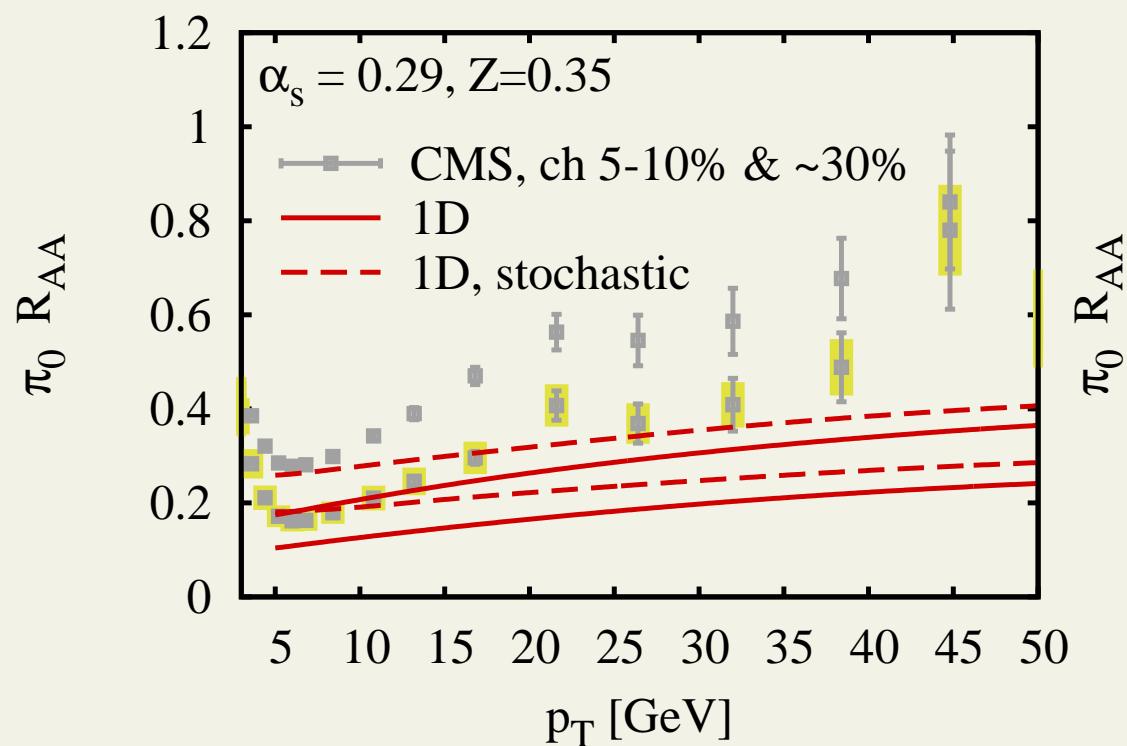
smaller v_2 with transverse expansion - GLV favors later times (large $\Delta z/\tau_f$)

Now move to LHC energies. Simple assumption:

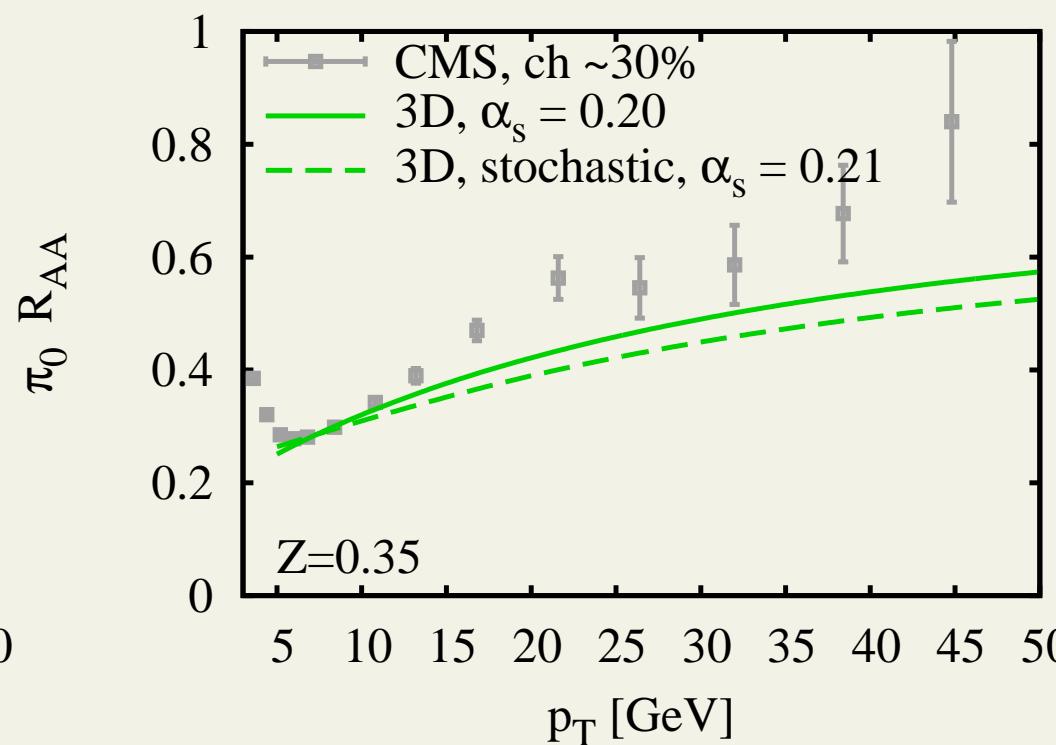
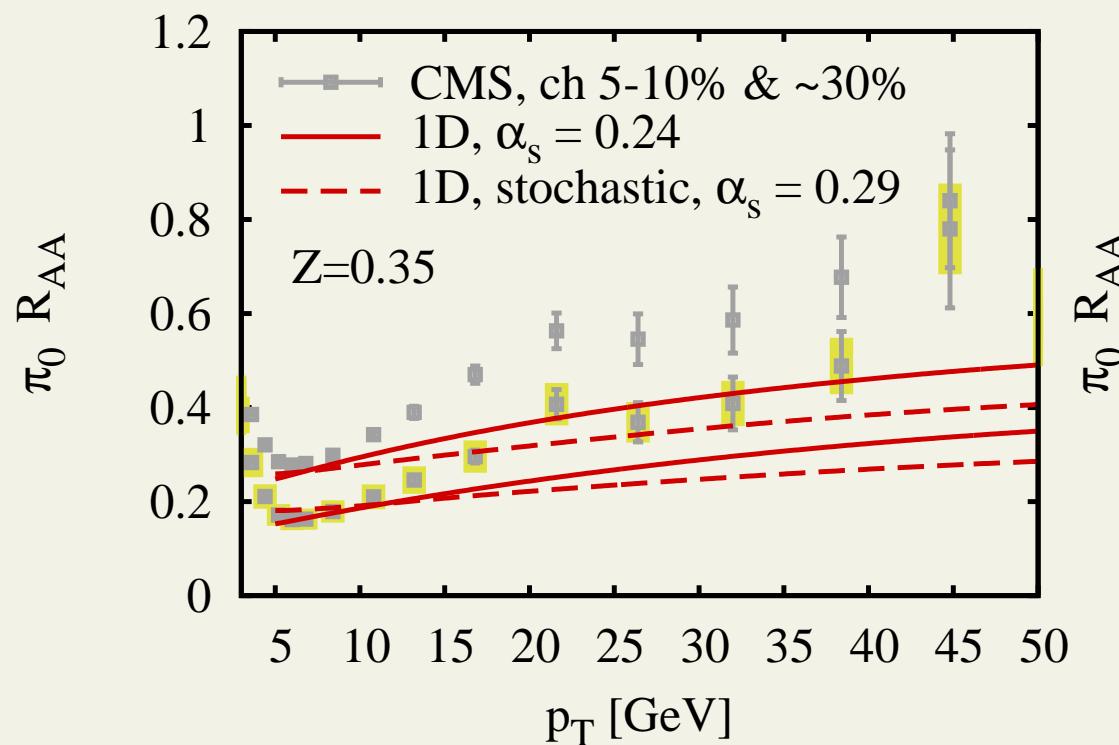
- higher $dN/d\eta = 2400$ in central collisions ($b = 0$)
- all other ingredients stay same

at present we only have mid-peripheral results in the 3D case

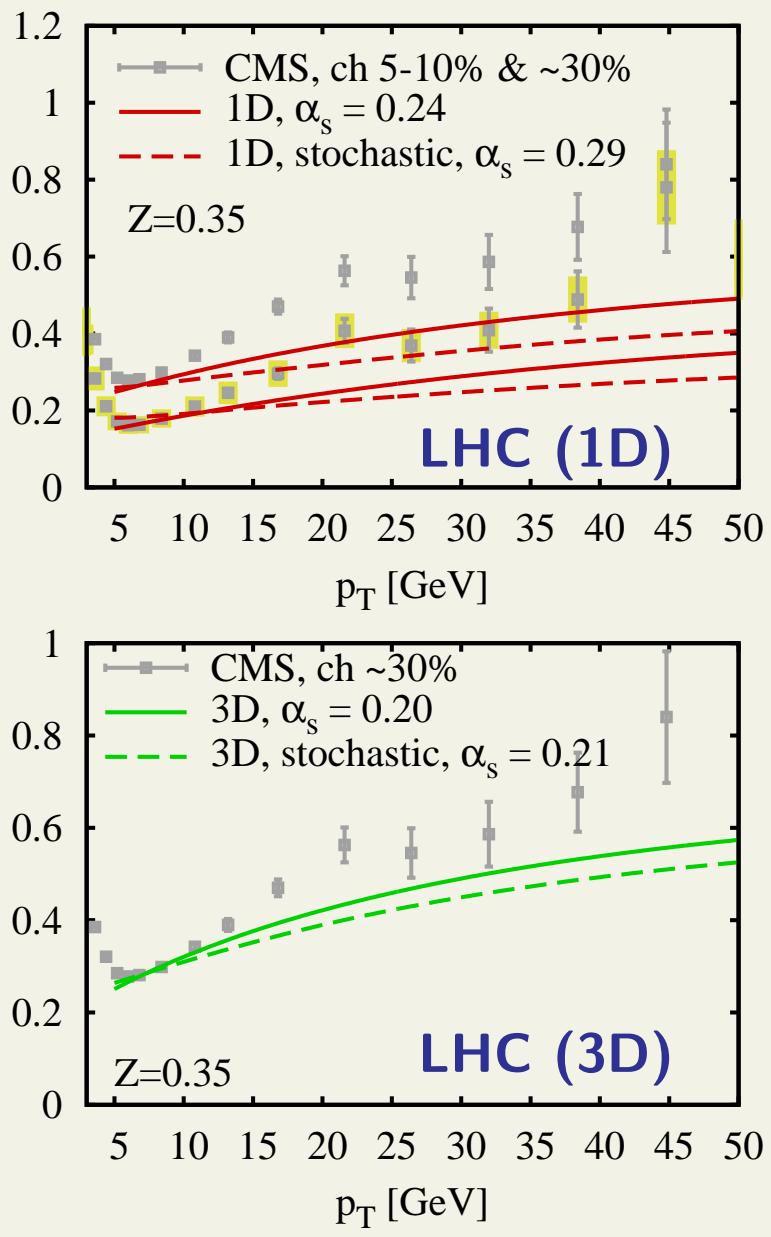
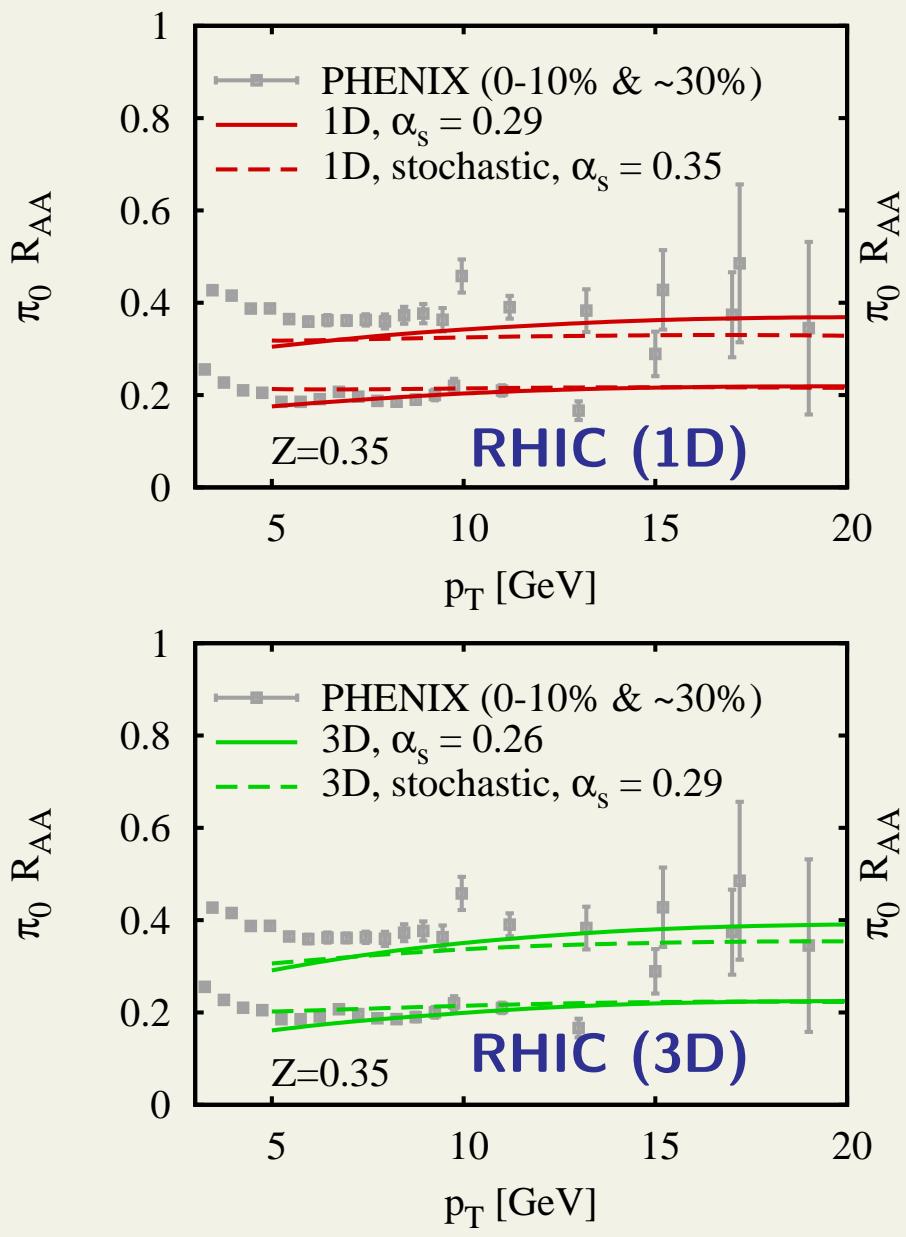
pion RAA, LHC



pion RAA, LHC - α_s scaled to RAA for central at $pT = 6$ GeV

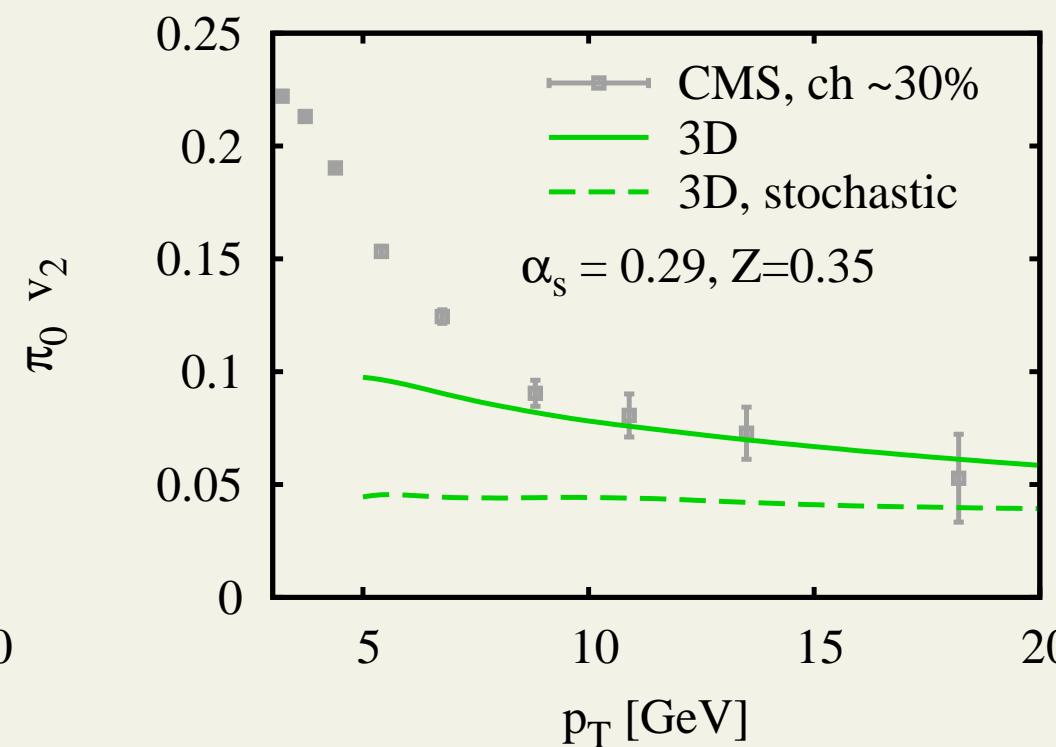
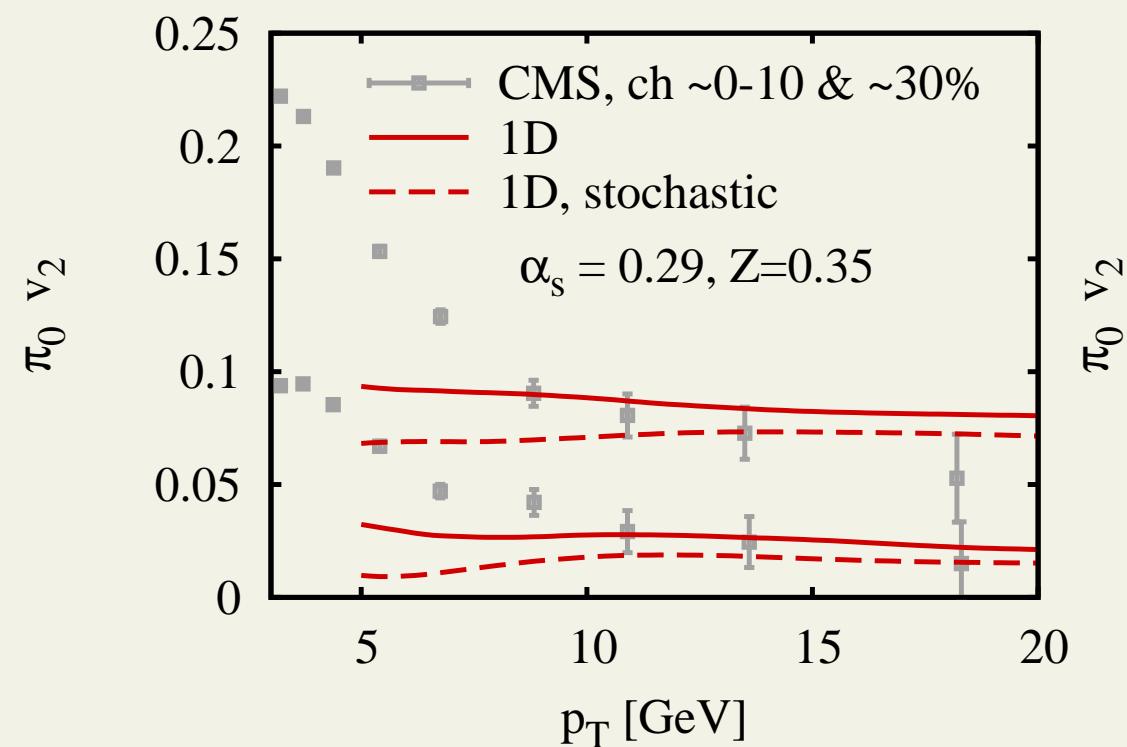


GLV implementation here is simplified, also $\alpha_s = const$ (no running)

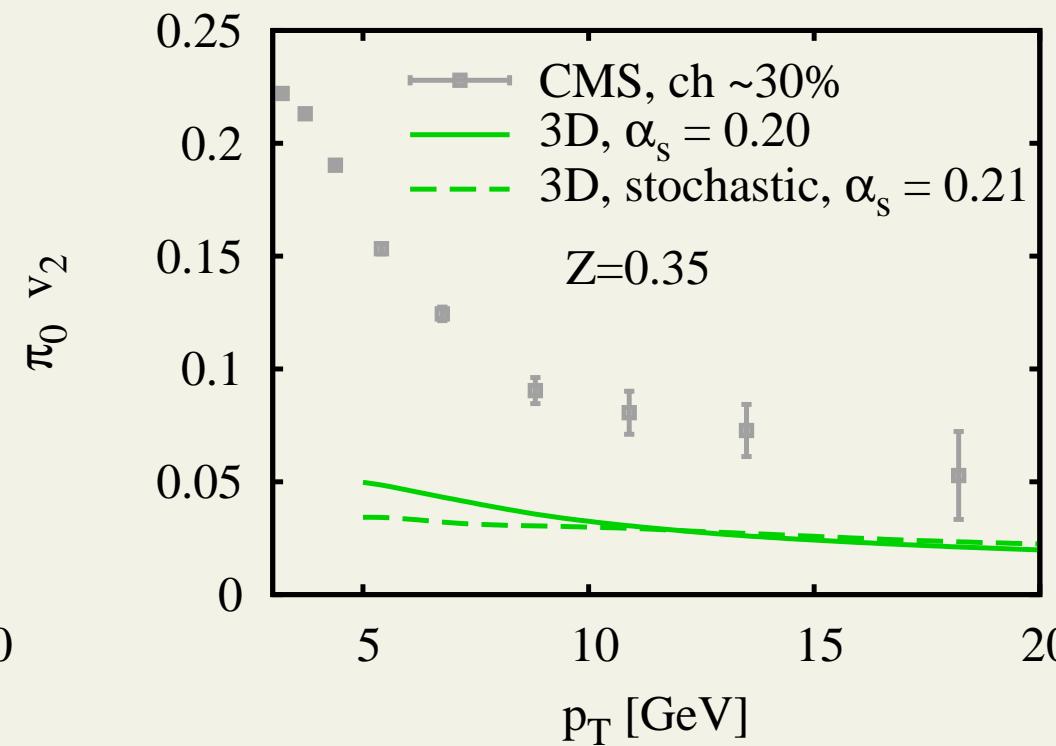
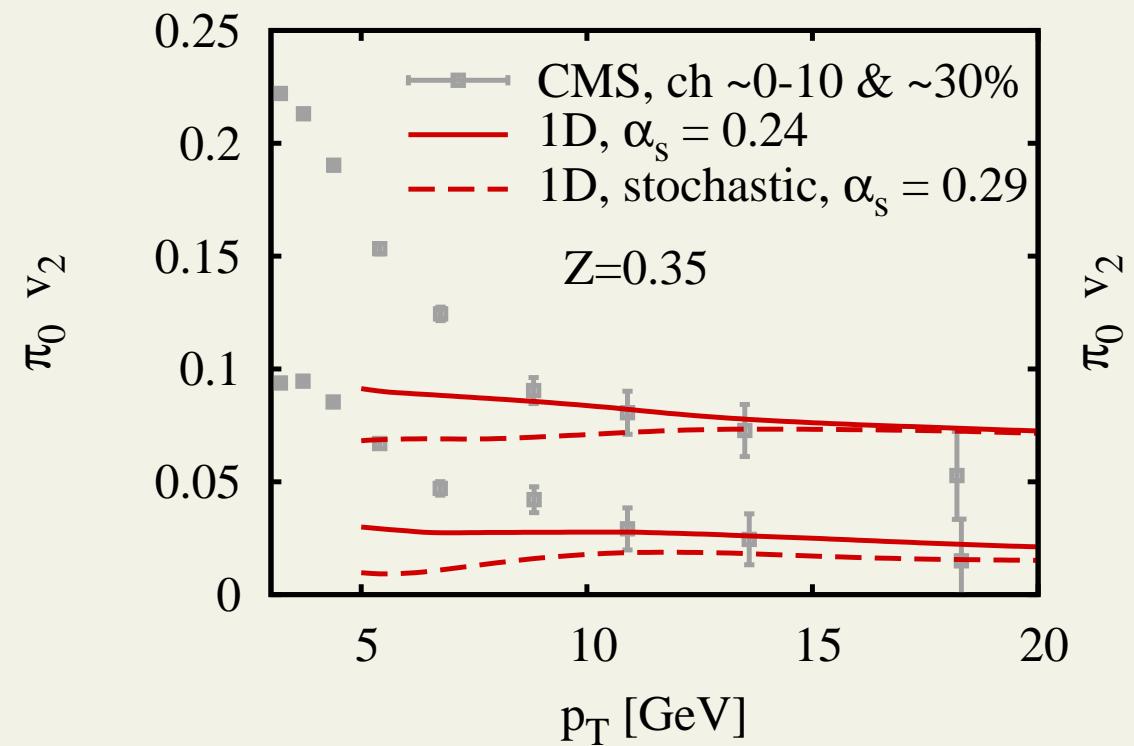


need 20 – 25% smaller α_s at LHC than at RHIC - similar to Betz et al, 1201.0281

pion v2, LHC

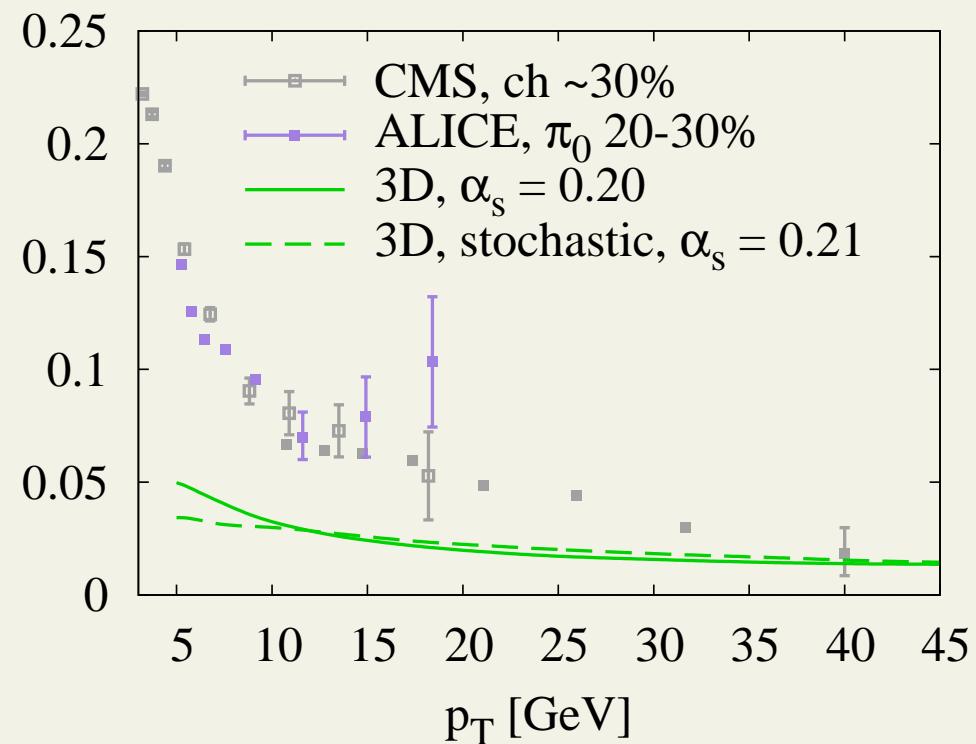
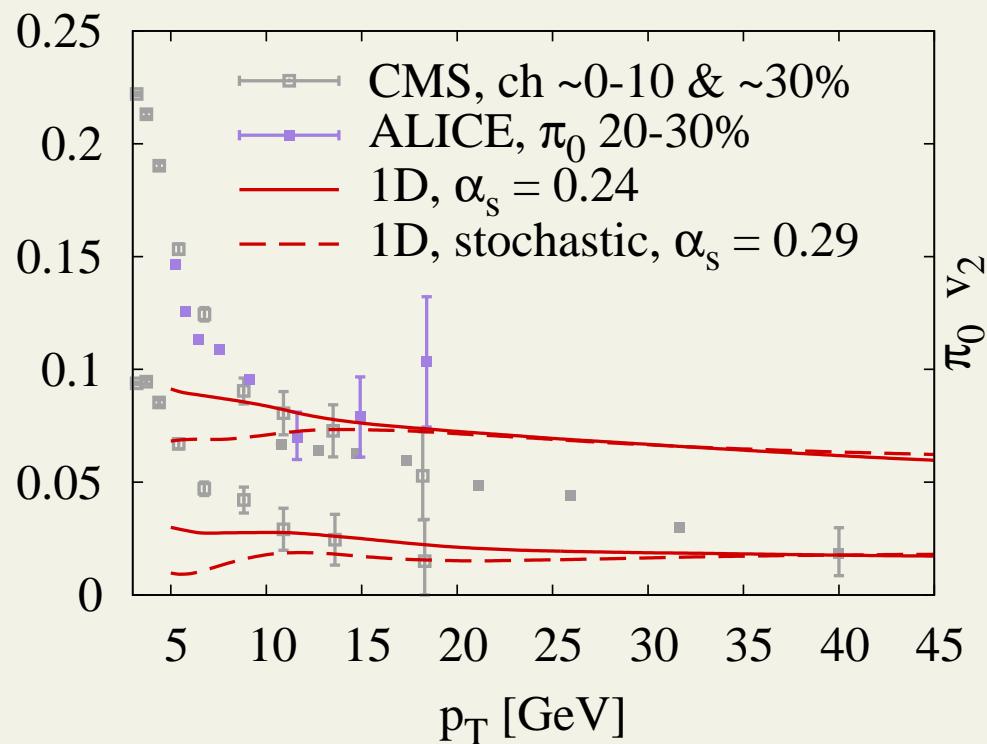


pion v2, LHC - α_s scaled to RAA at $pT = 6$ GeV



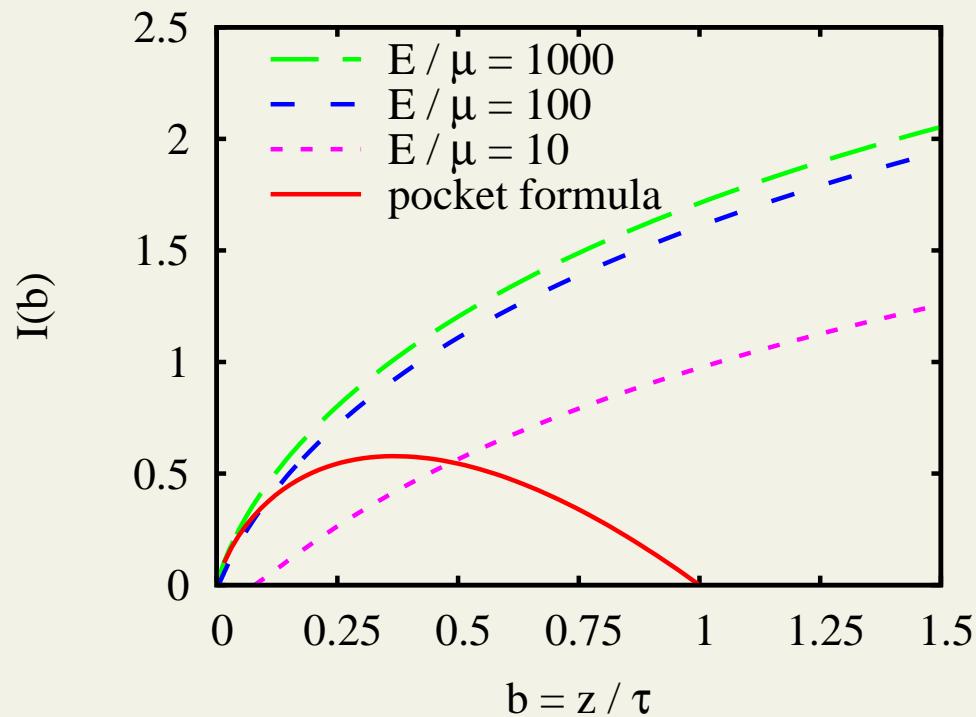
similar reduction in 3D case as at RHIC energies

high-pT pion v2, LHC (α_s scaled to RAA at $pT = 6$ GeV)



In short: for transversely expanding medium, both R_{AA} and v_2 are smaller with GLV energy loss. LPM interference favors late scattering.

$$\Delta E_{GLV}^{(1)}(z) \propto \int dx dk dq \frac{\mu^2}{\pi(q^2 + \mu^2)^2} \frac{2k \cdot q}{k^2(k - q)^2} (1 - \cos \omega \Delta z) \propto I(\Delta z / \tau(z), E / \mu(z))$$

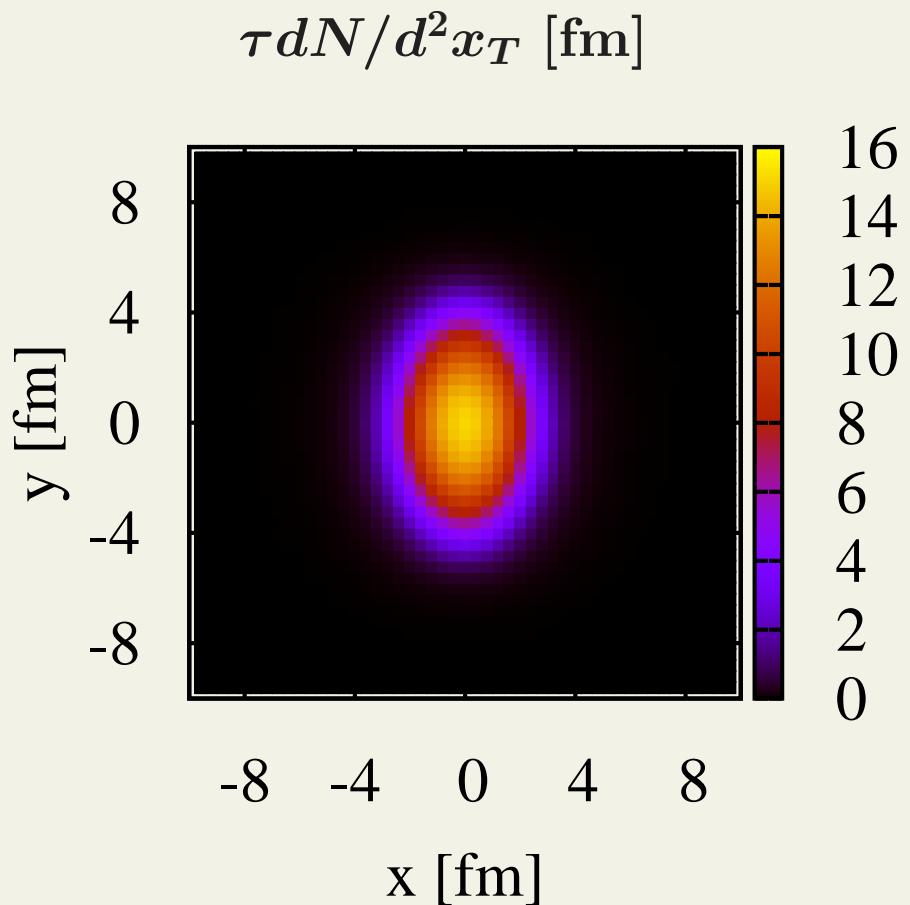


$$\tau(z) \equiv \frac{2E}{\mu^2(z)}$$

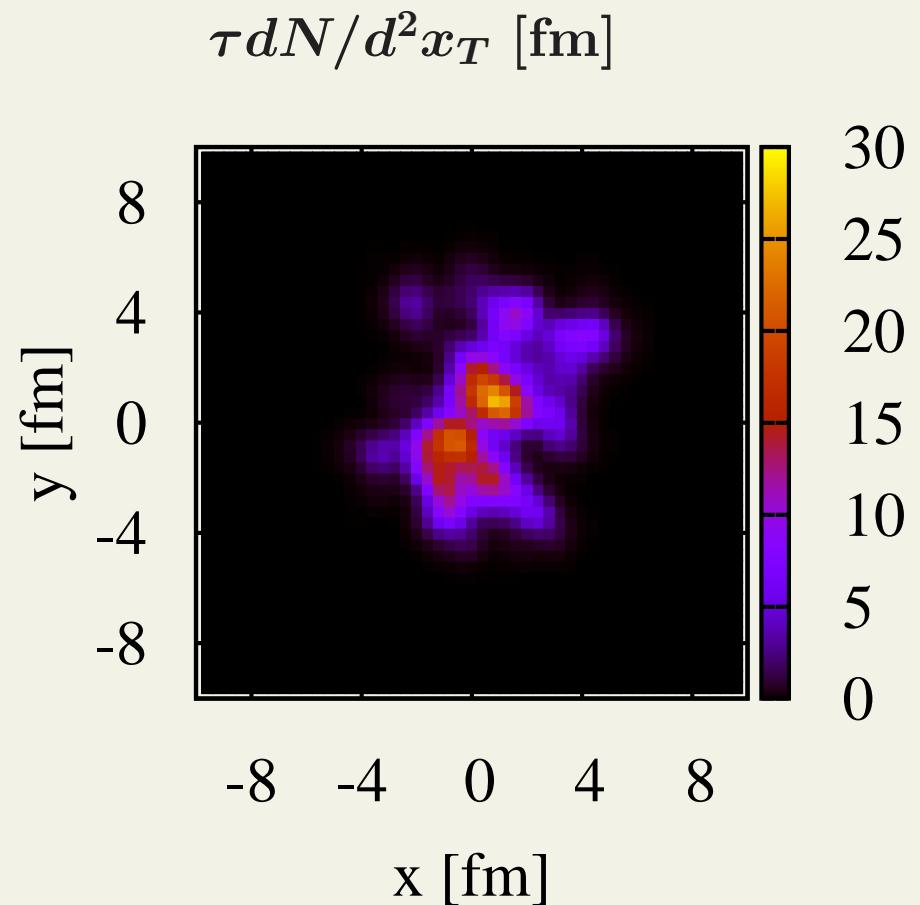
Could fluctuations help?

- MC Glauber initconds (binary)
- RHIC Au+Au at $b = 8$ fm, $200A$ GeV
- same $2 \rightarrow 2$ transport (MPC)

average Au+Au, b=8 fm

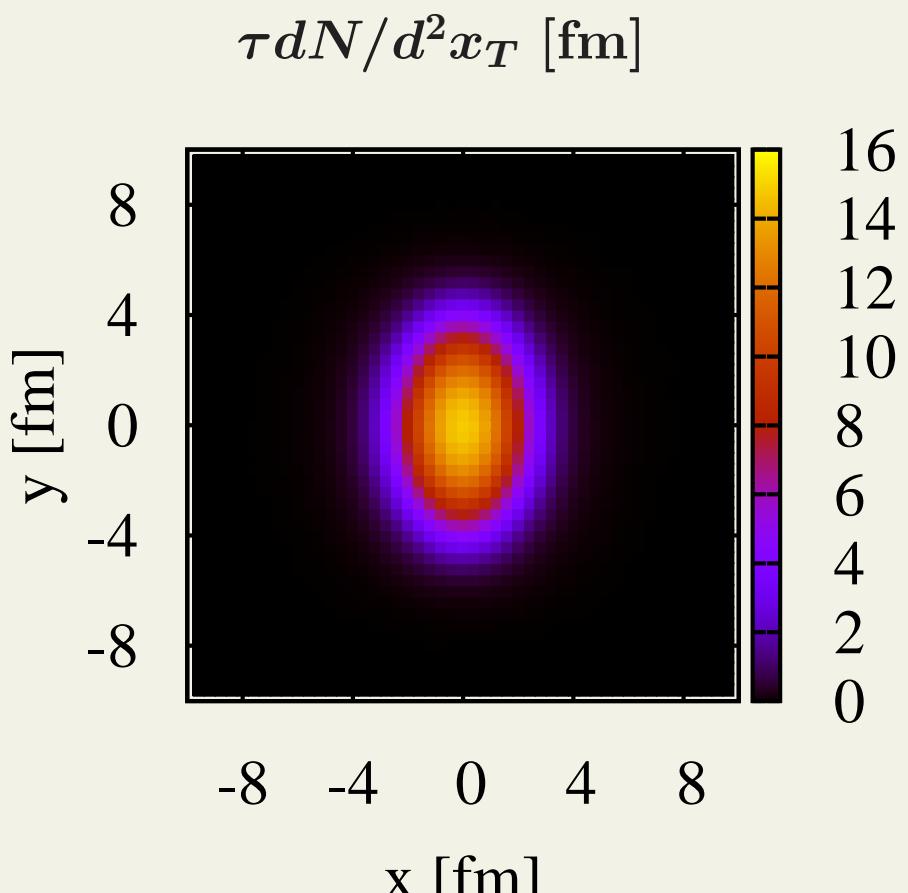


single MC Glauber

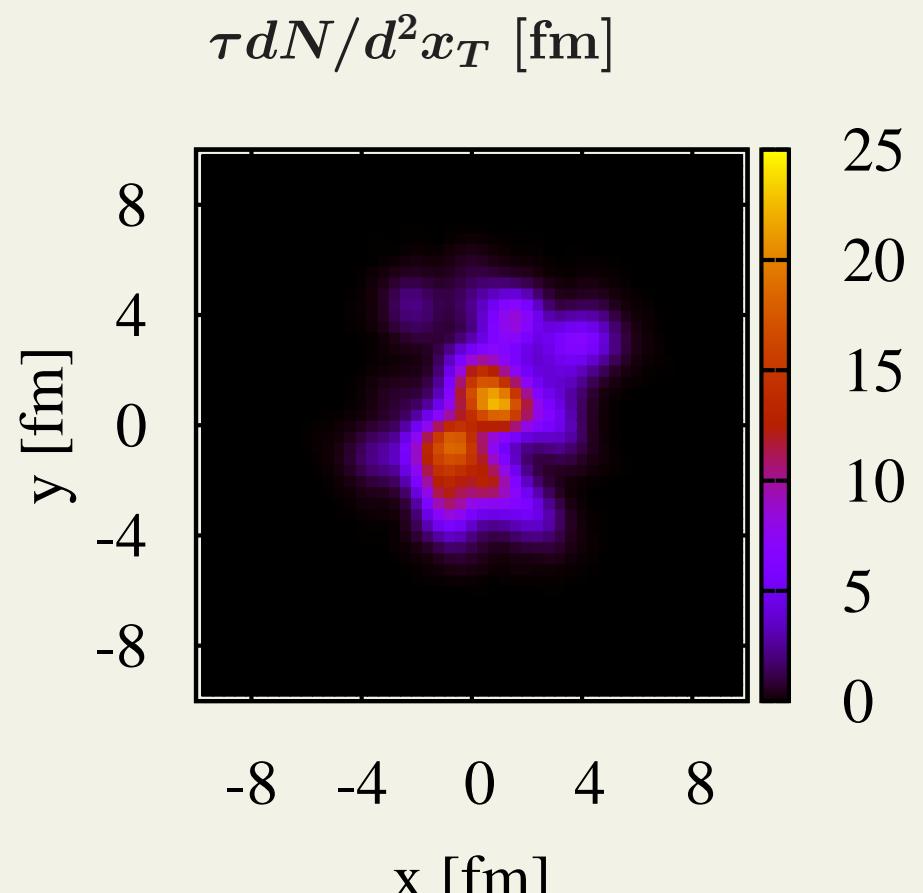


$\tau = 0.6$ fm

average Au+Au, $b=8$ fm

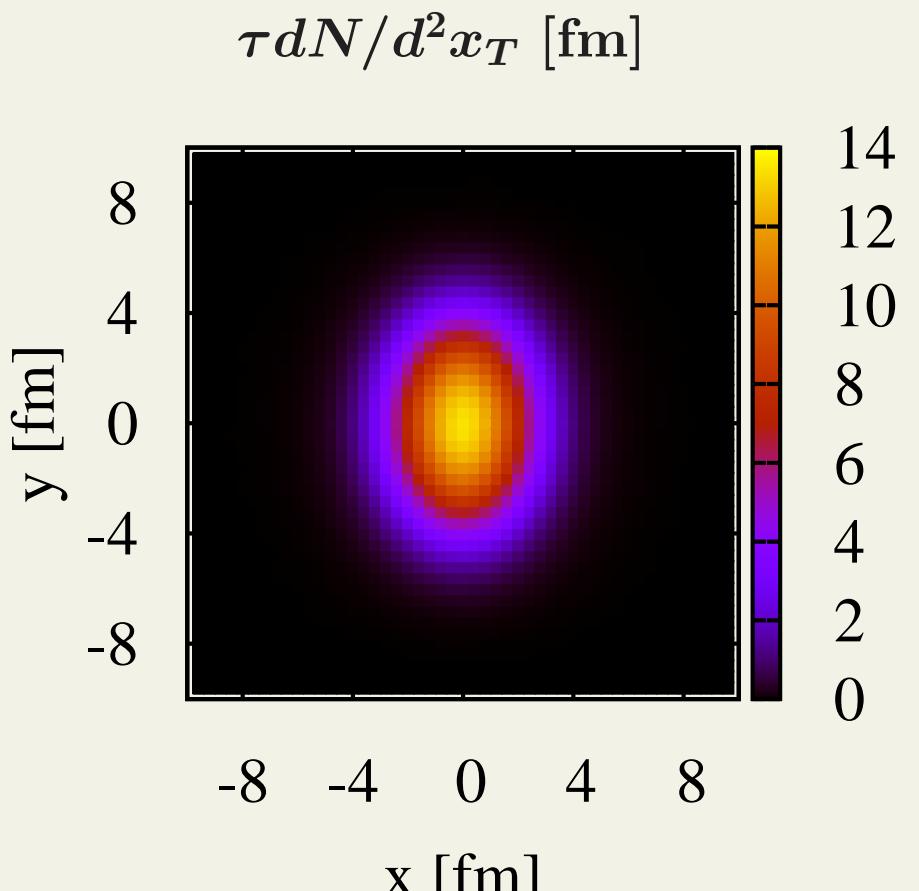


single MC Glauber

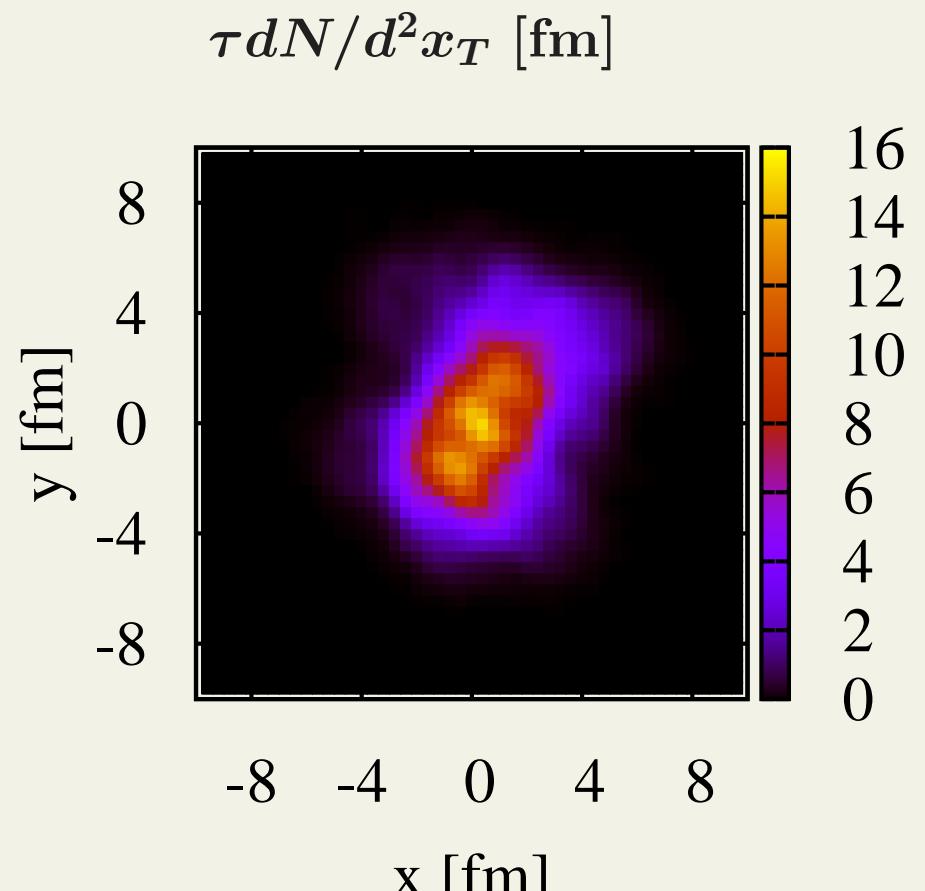


$\tau = 1.2$ fm

average Au+Au, $b=8$ fm

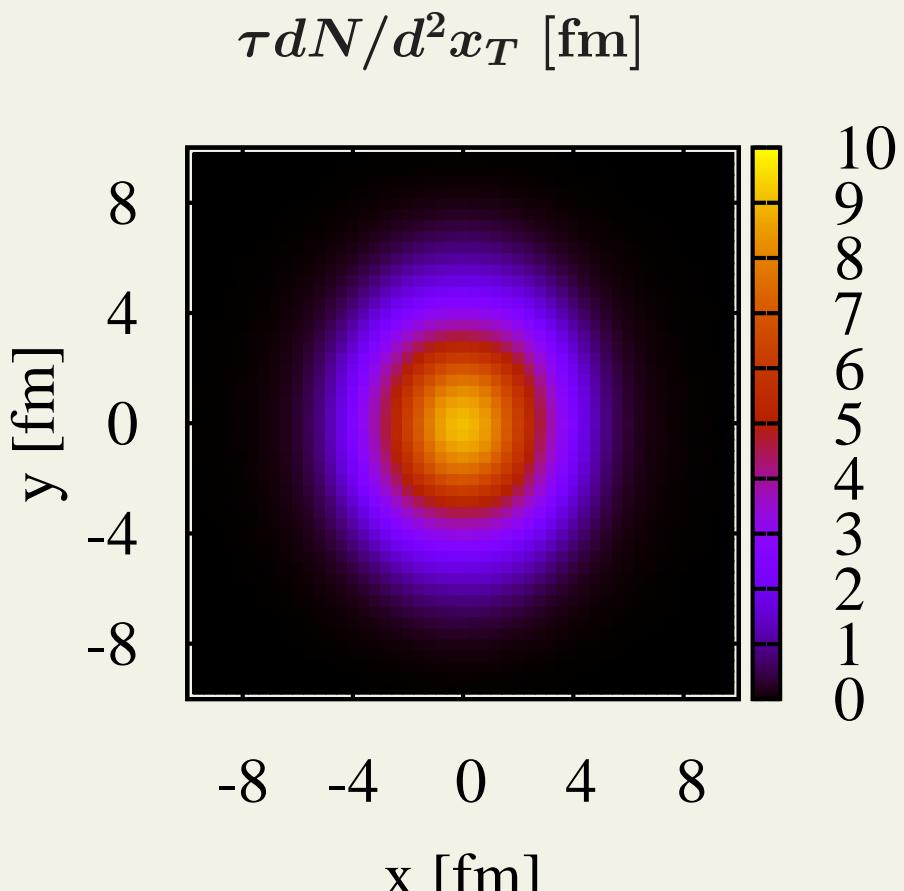


single MC Glauber

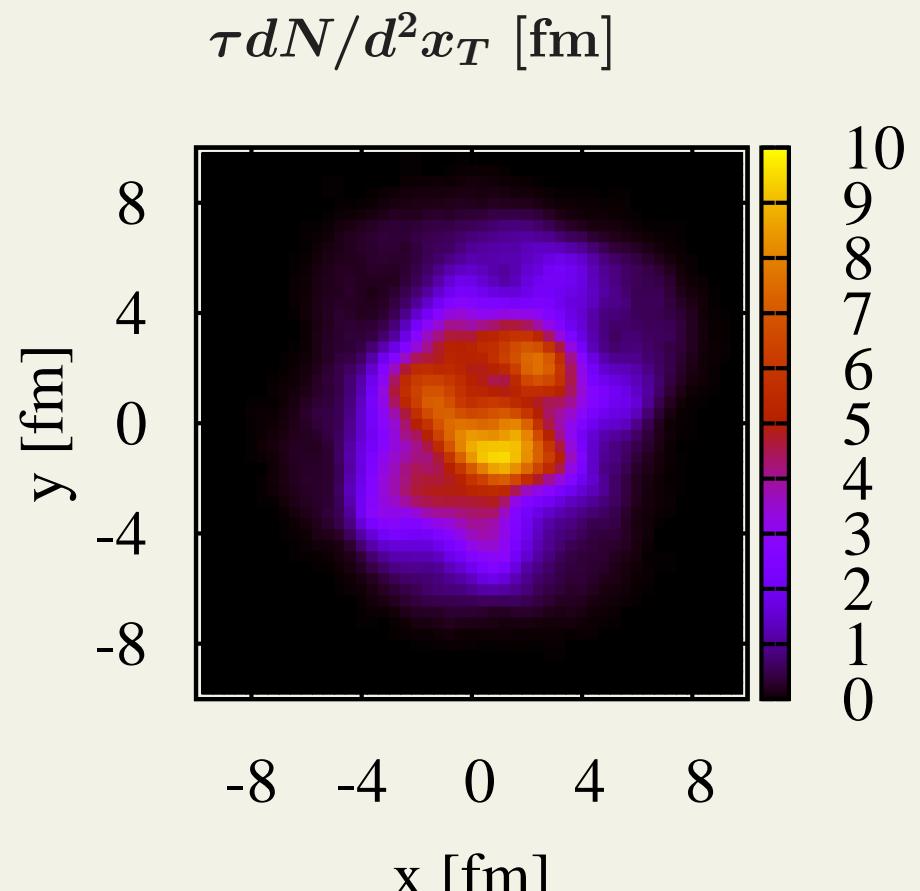


$\tau = 2.1$ fm

average Au+Au, $b=8$ fm

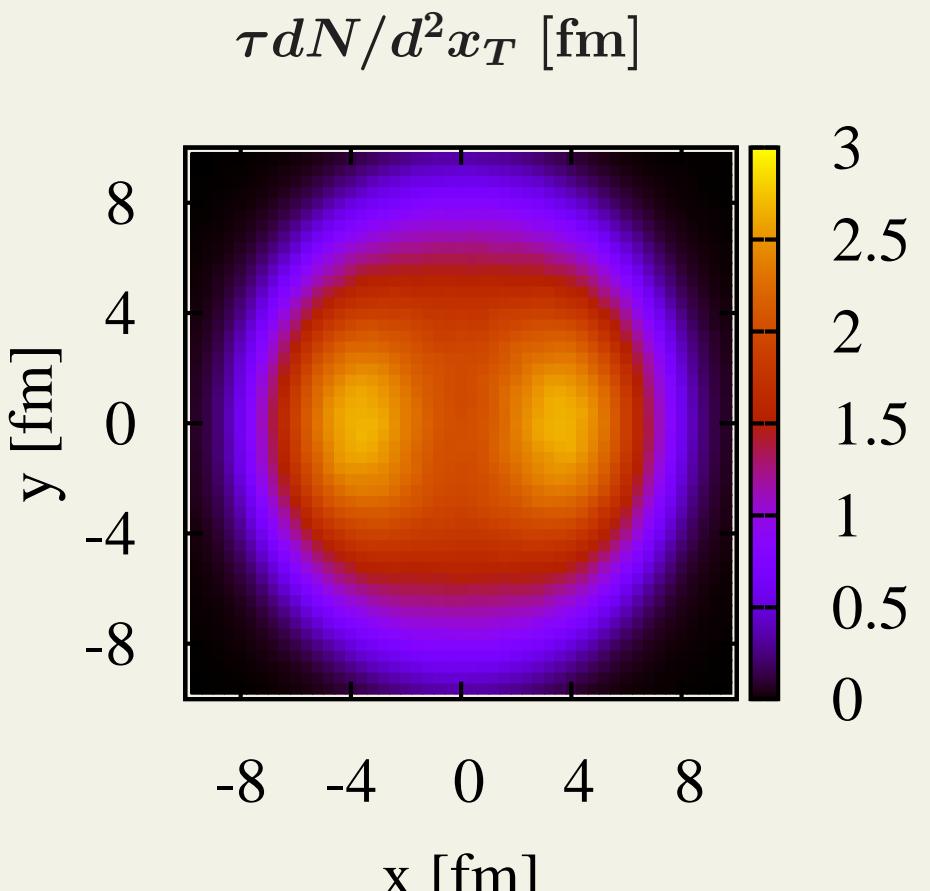


single MC Glauber

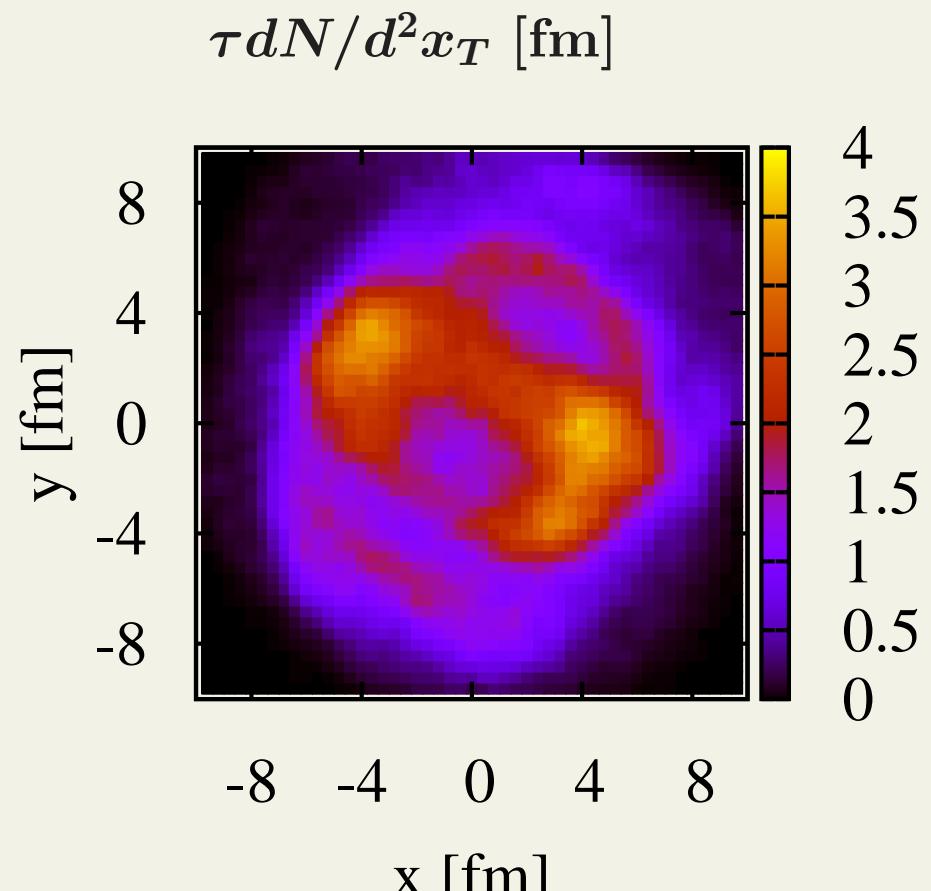


$\tau = 3.6$ fm

average Au+Au, $b=8$ fm

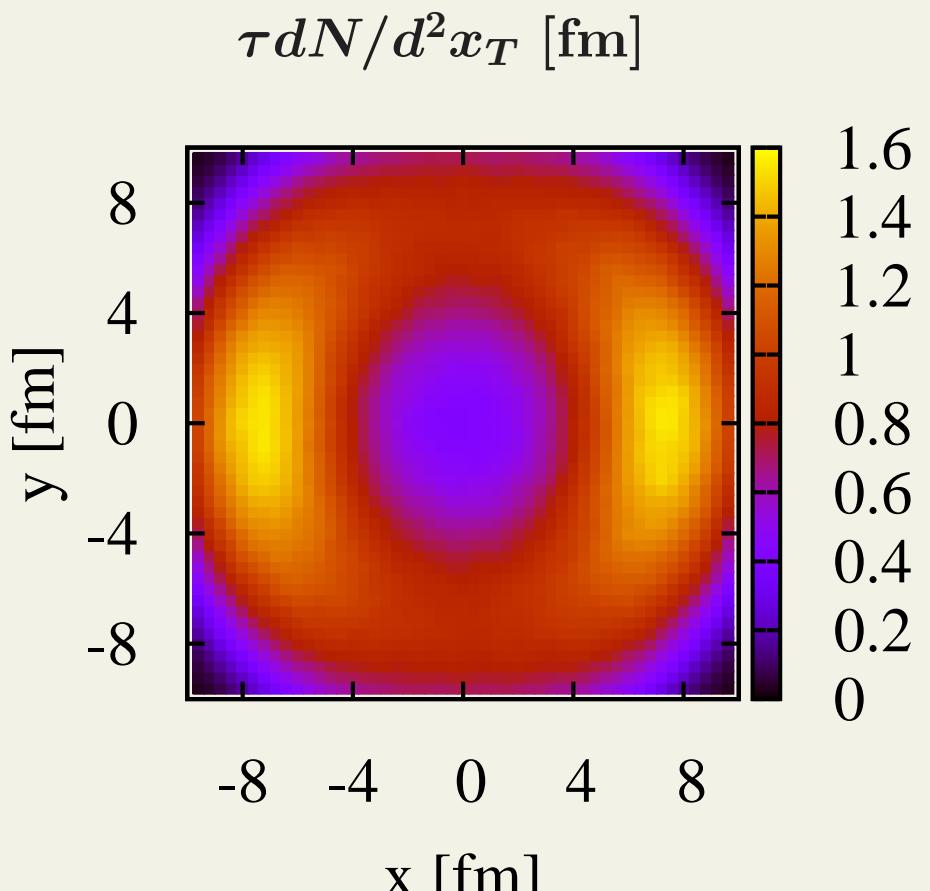


single MC Glauber

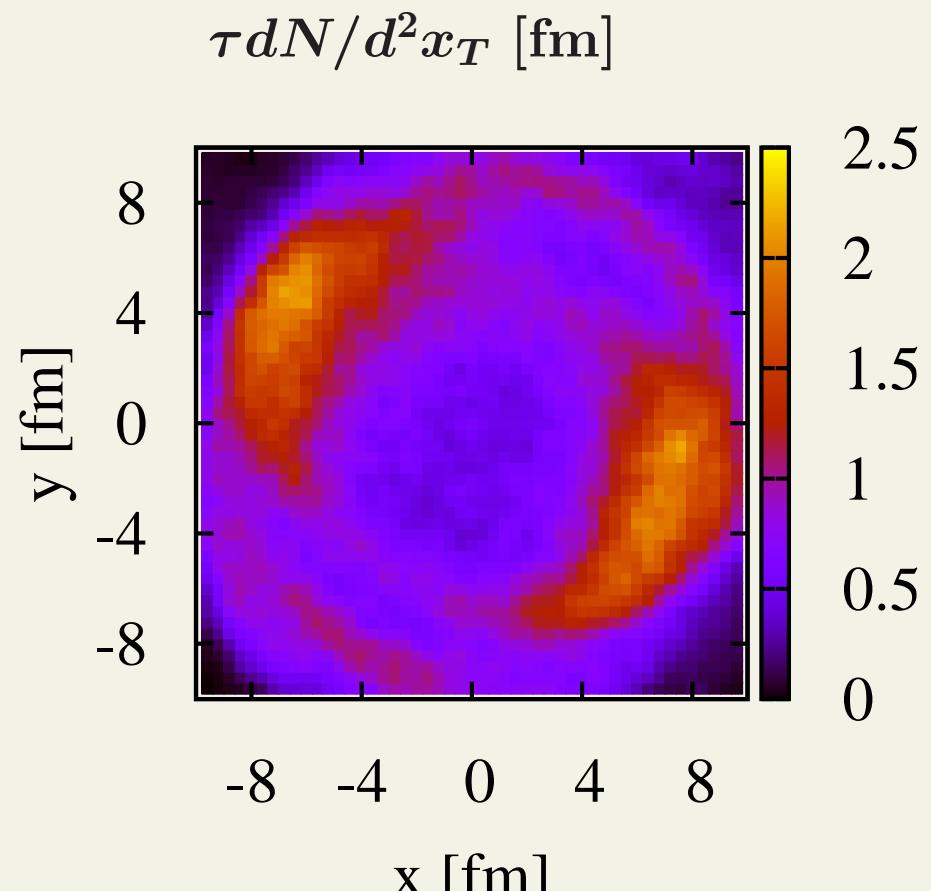


$\tau = 6.6$ fm

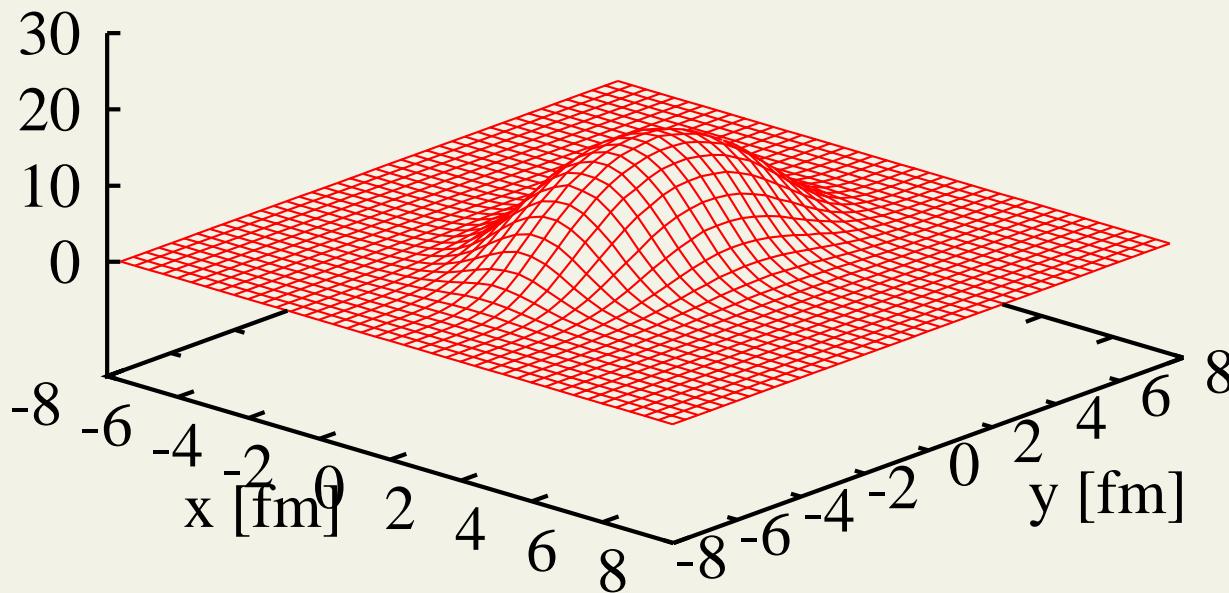
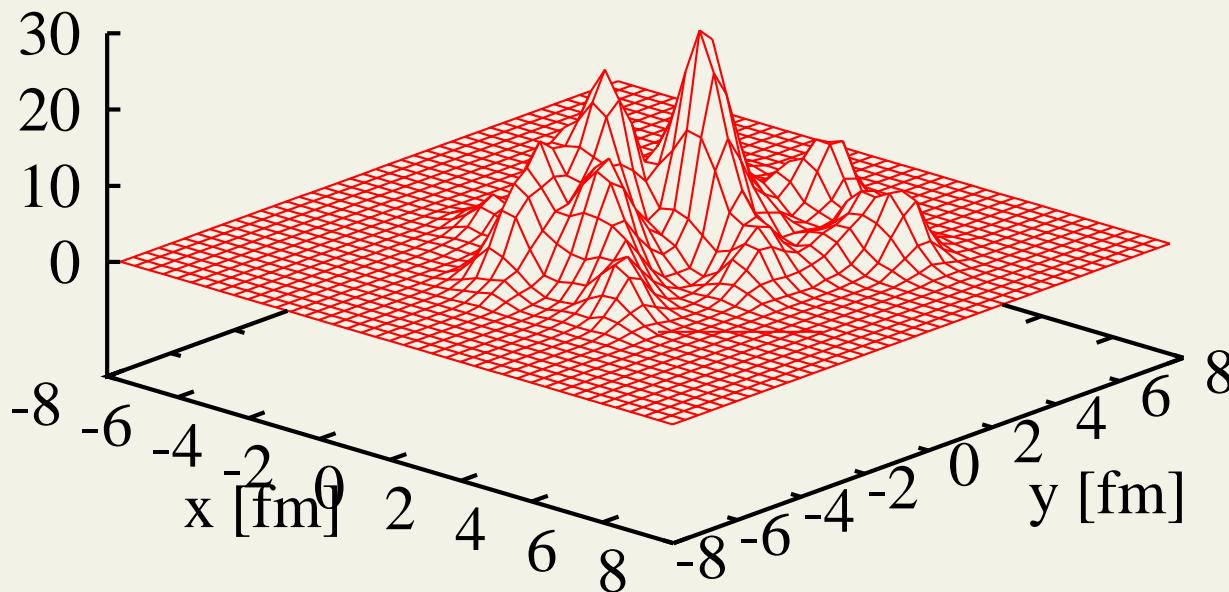
average Au+Au, $b=8$ fm



single MC Glauber



$\tau = 9.6$ fm

$\tau n [fm^2]$  $\tau n [fm^2]$ 

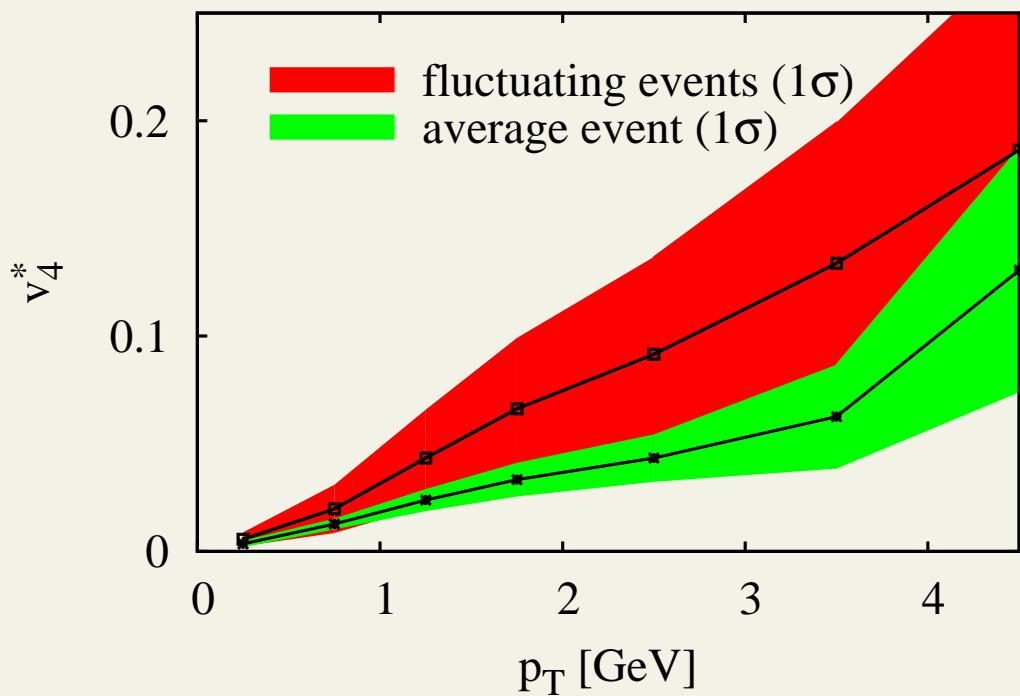
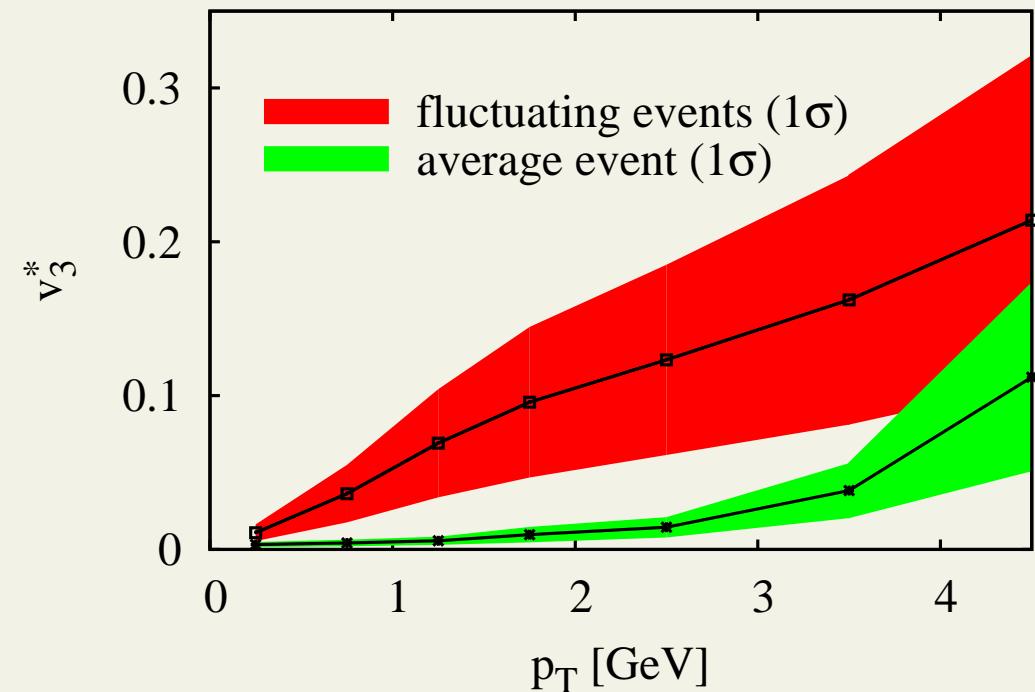
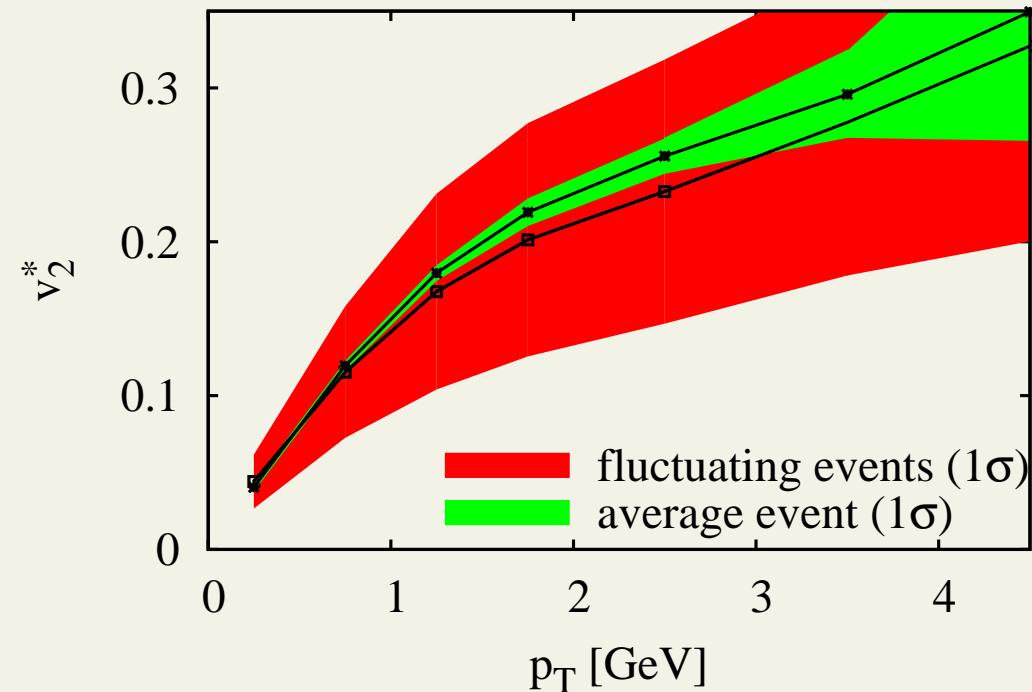
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Analyze MEDIUM and JET response using eccentricity coefficients

$$\begin{aligned}\vec{\epsilon}_{n,k} &\equiv \frac{1}{\langle r^k \rangle} (\langle r^k \cos(n\phi_x) \rangle, \langle r^k \sin(n\phi_x) \rangle) \\ &= \epsilon_{n,k}^* (\cos \Phi_{n,k}, \sin \Phi_{n,k})\end{aligned}$$

and similar decomposition for transverse momenta (v_n, Φ_n)

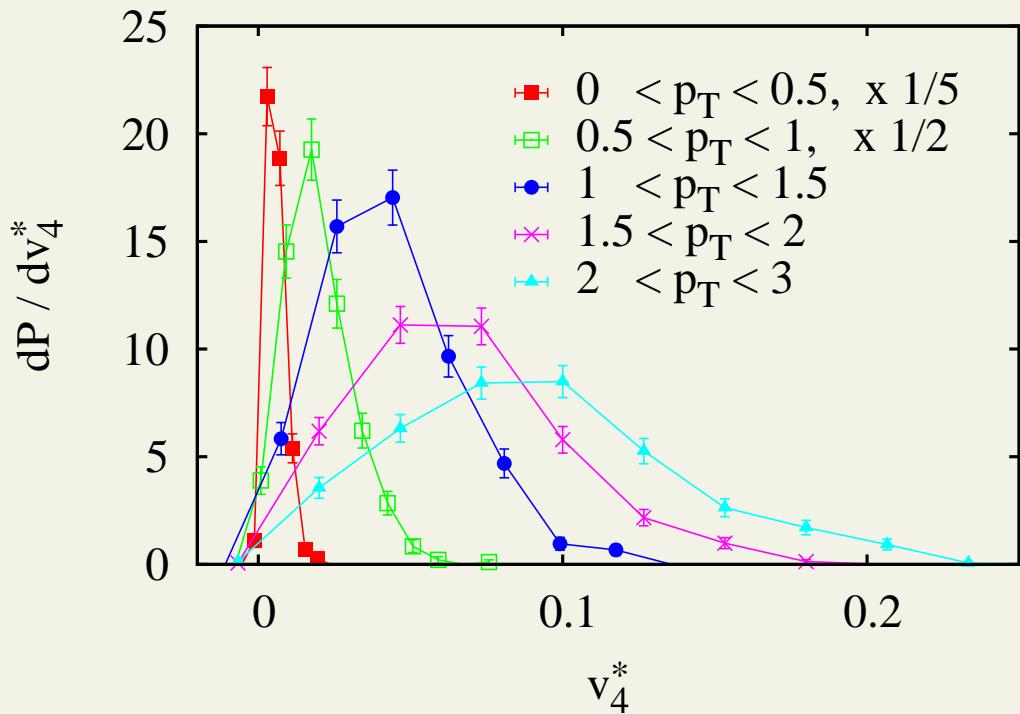
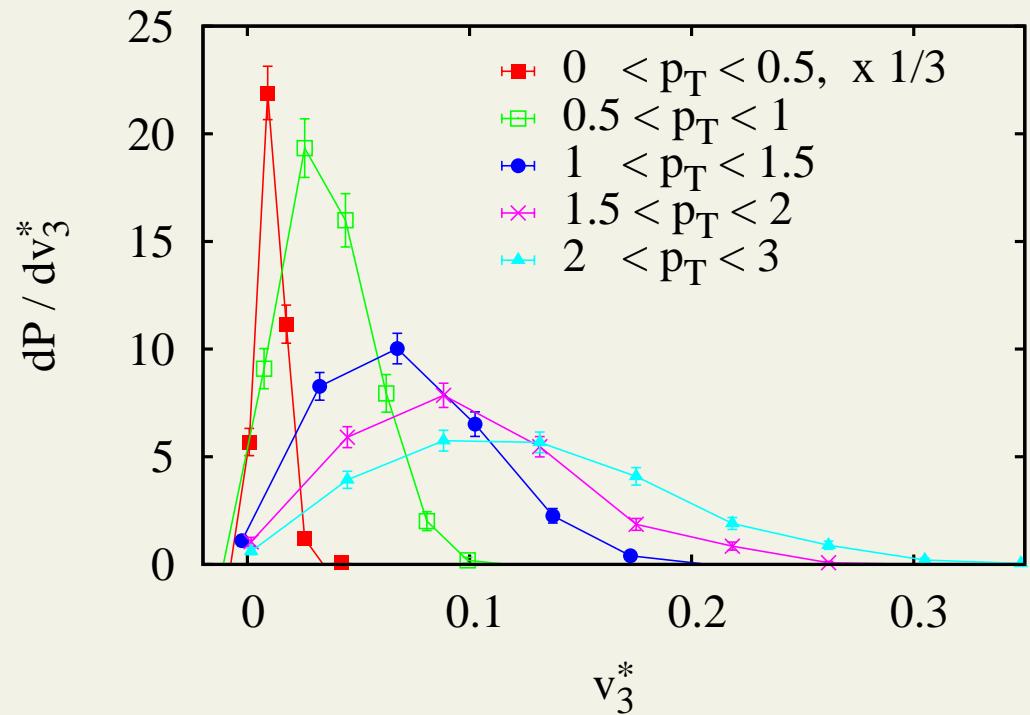
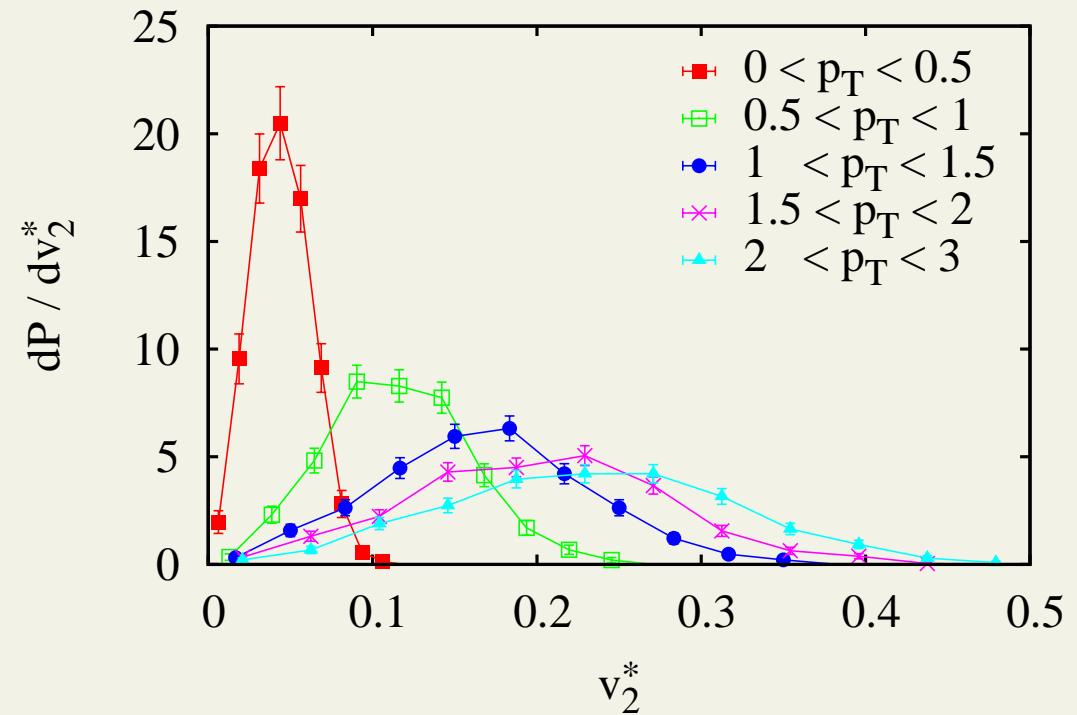
$$\frac{dN}{d\varphi} \propto 1 + \sum_{n=1}^{\infty} 2v_n \cos n(\varphi - \Phi_n)$$



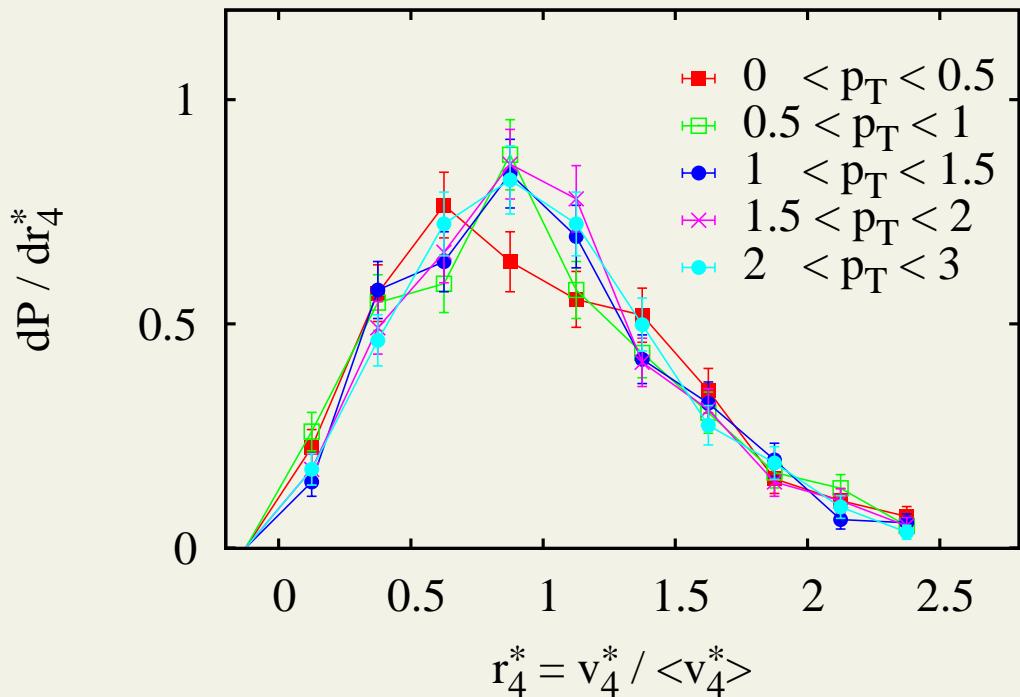
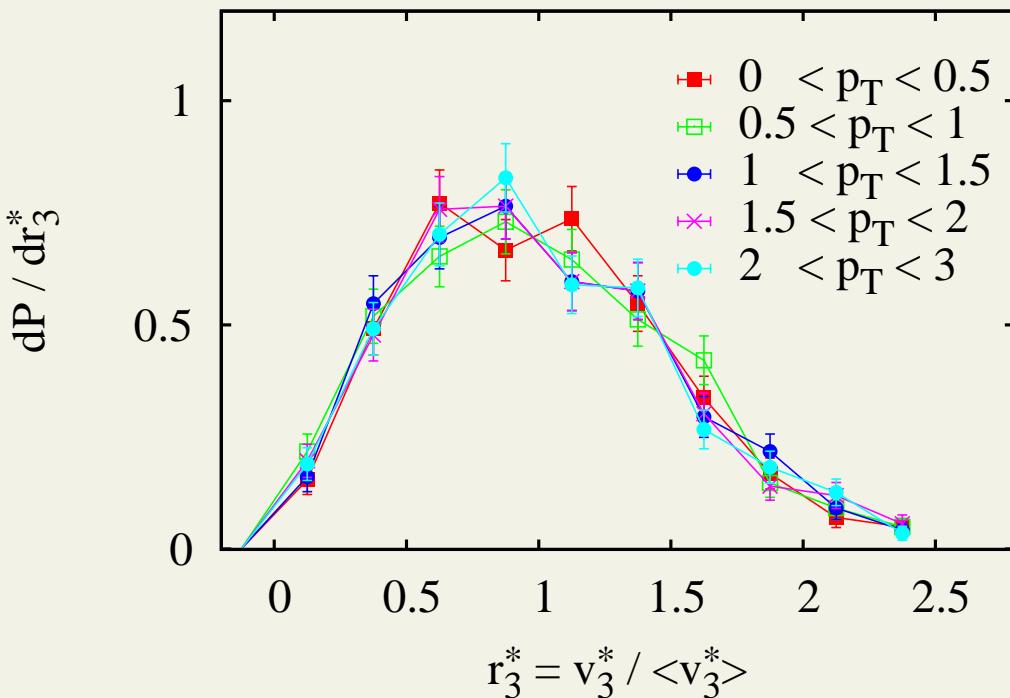
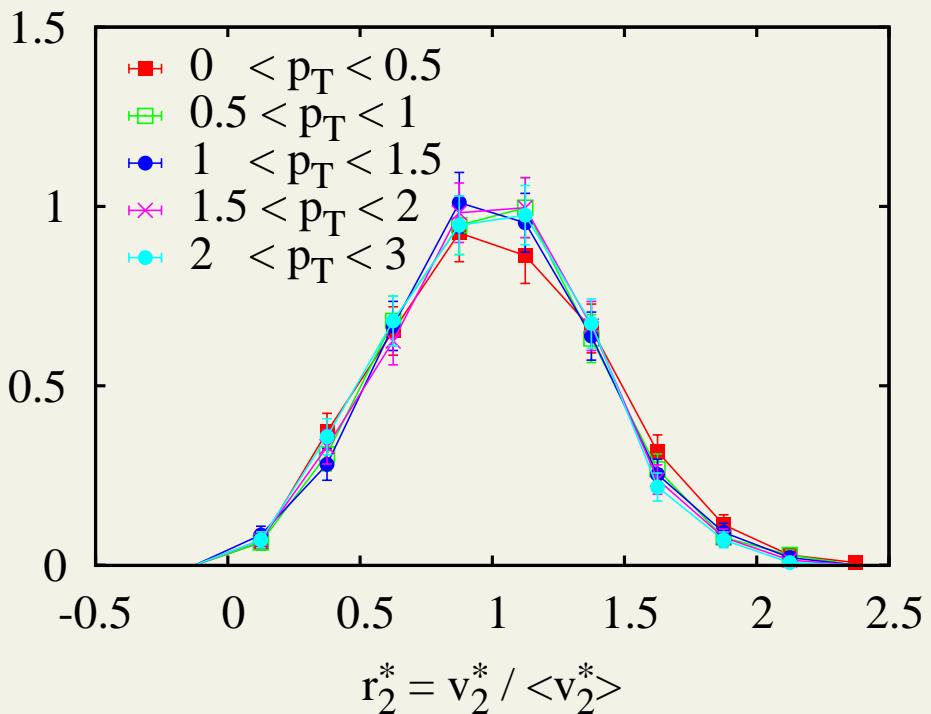
average v_2 essentially same as from averaged initcond

v_n increase with p_T

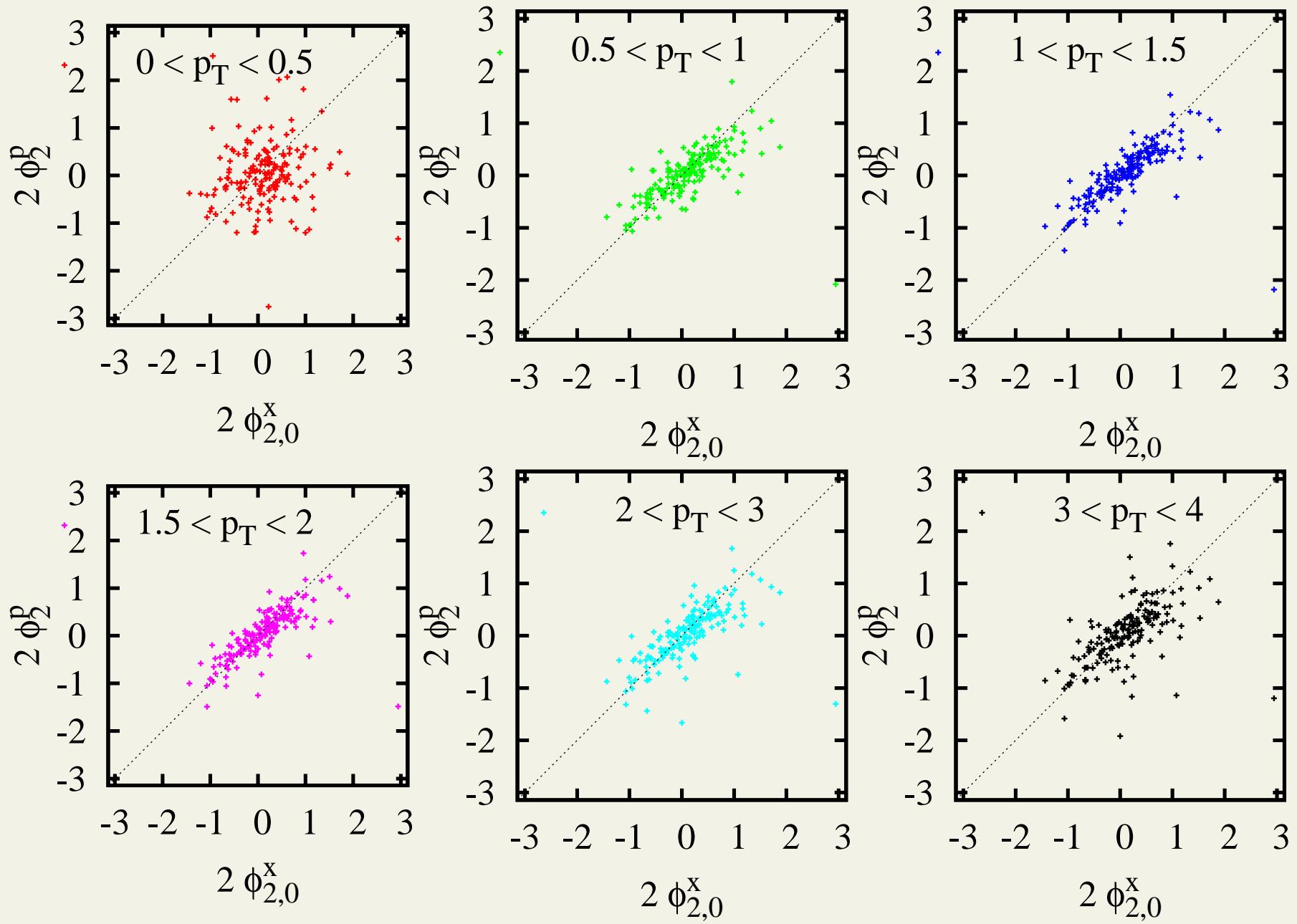
(shades represent $\sqrt{\langle \delta v_n^2 \rangle}$)

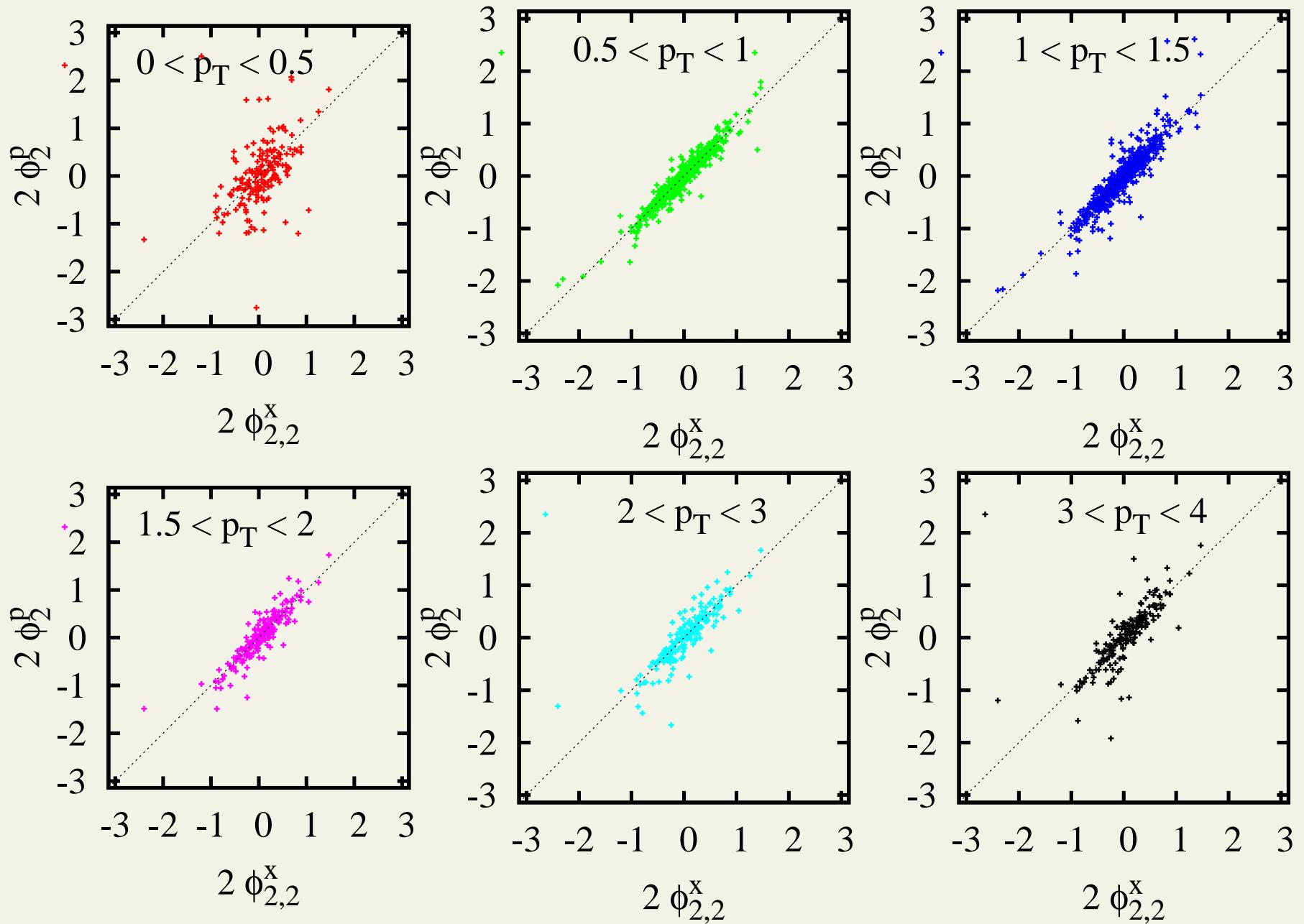


**MC Glauber initial conditions
induce large v_2 , v_3 , v_4
fluctuations in bulk transport
medium**

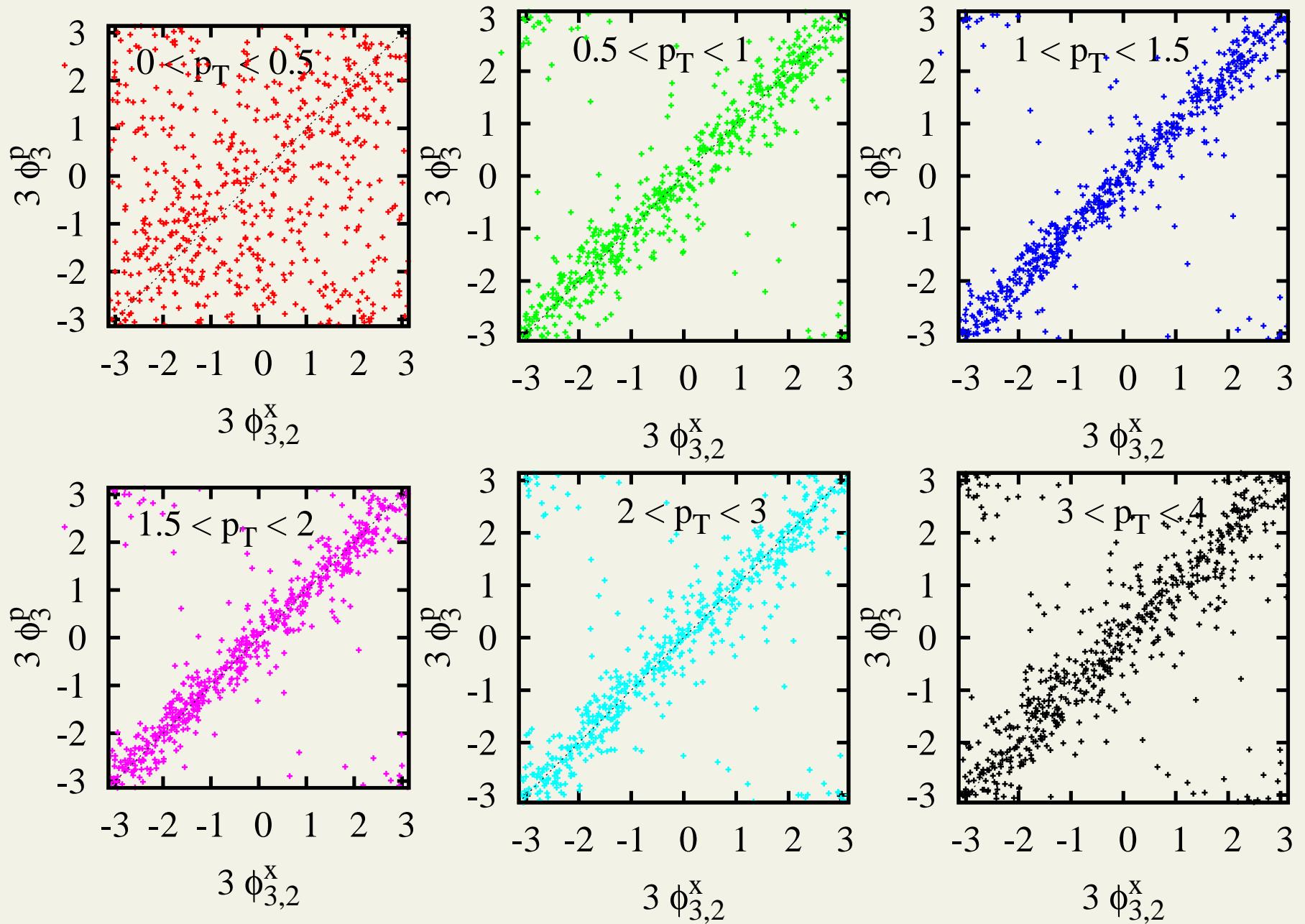


$v_n / \langle v_n \rangle$ nearly universal
independent of p_T





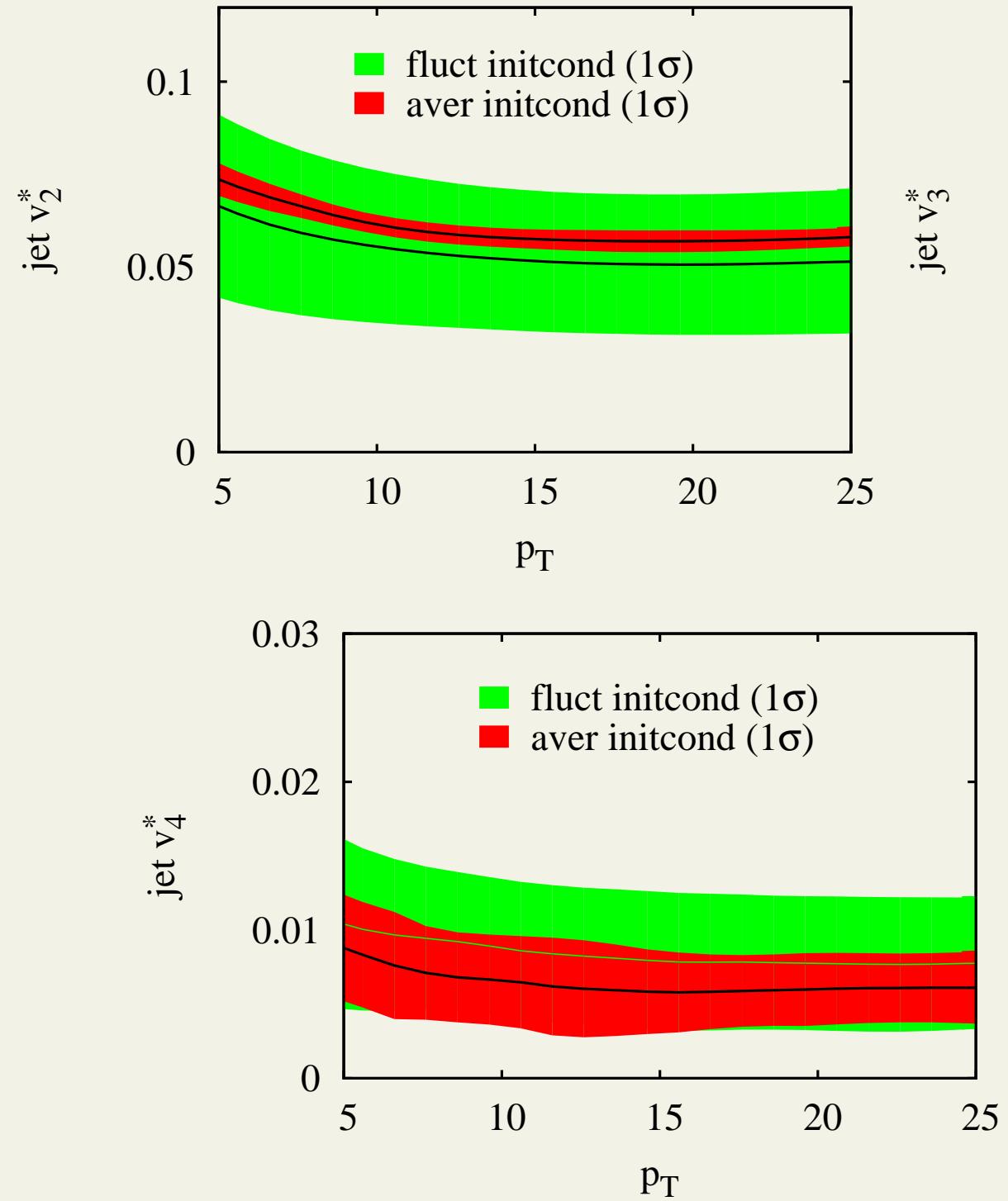
$\epsilon_{2,2}$ orientation correlates best with v_2 orientation



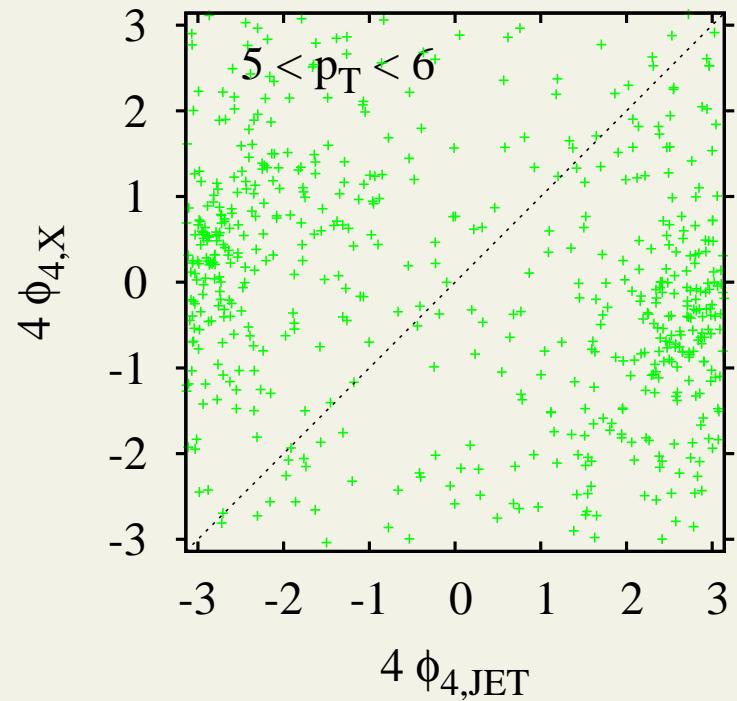
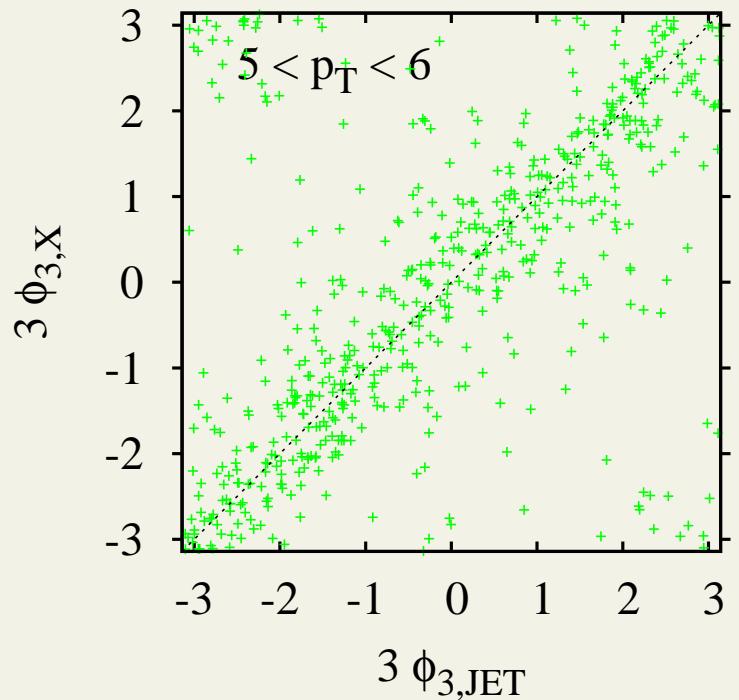
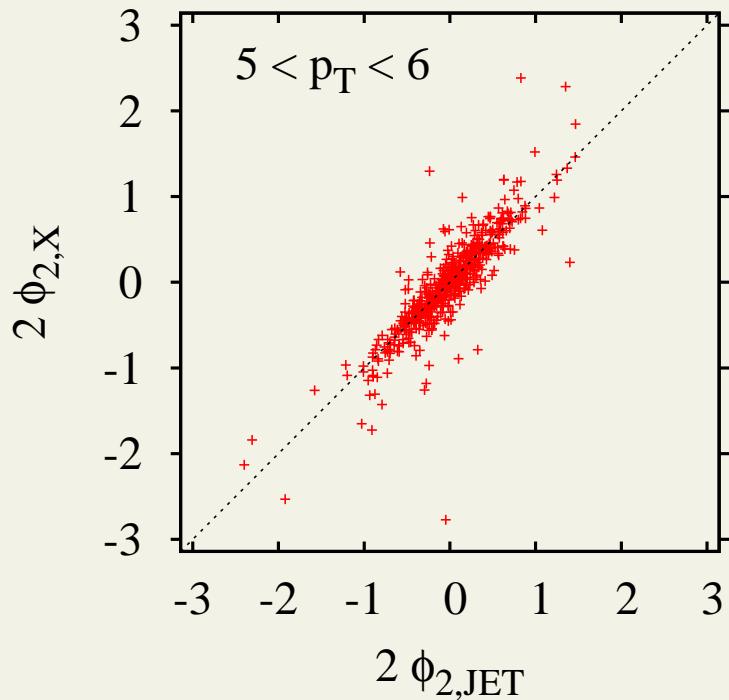
$\epsilon_{3,2}$ correlates strongly with v_3 orientation

Bulk medium response qualitatively similar to hydrodynamics.

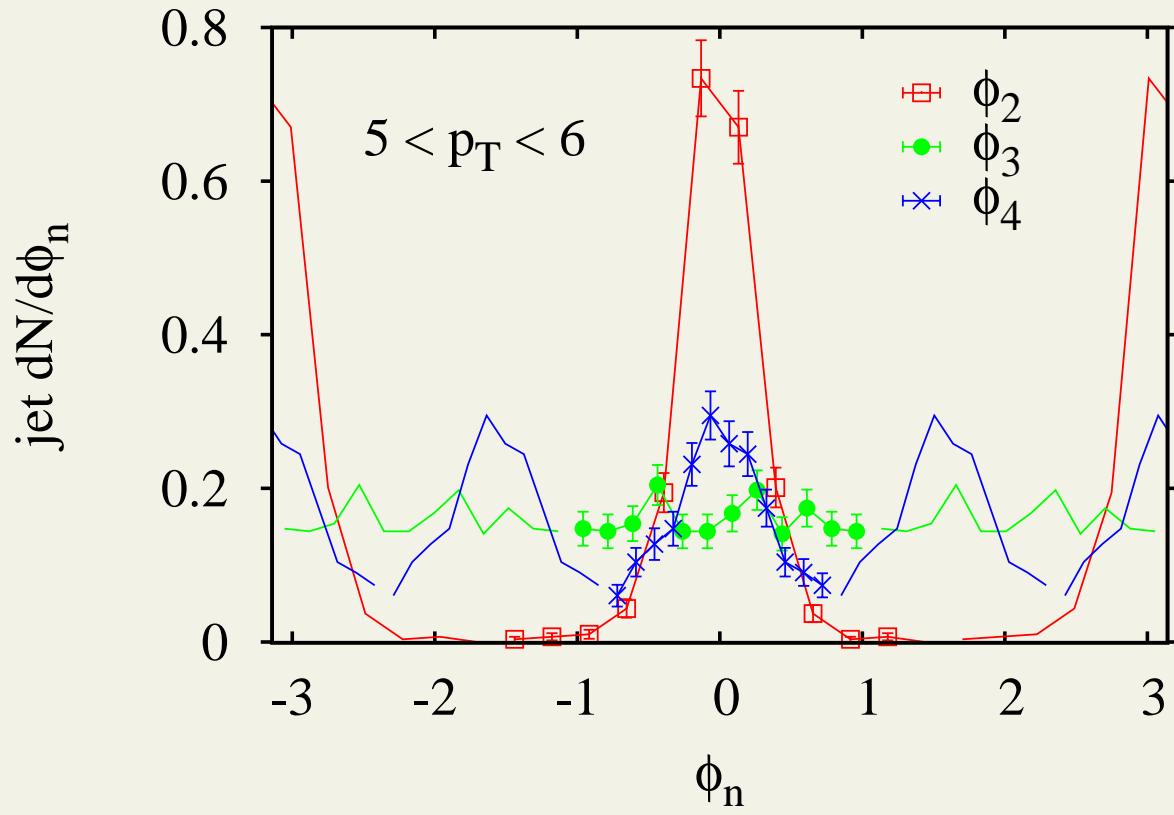
What about the jets?



**noticeable fluctuations in
jet v_n**



**JET v_2 and v_3 correlate
with orientation of $\epsilon_{2,3}$**



angles relative to theorist's reaction plane \rightarrow positive v_4

Summary

Parton transport can serve as bulk medium model. It responds to fluctuating initial conditions similarly to hydrodynamics.

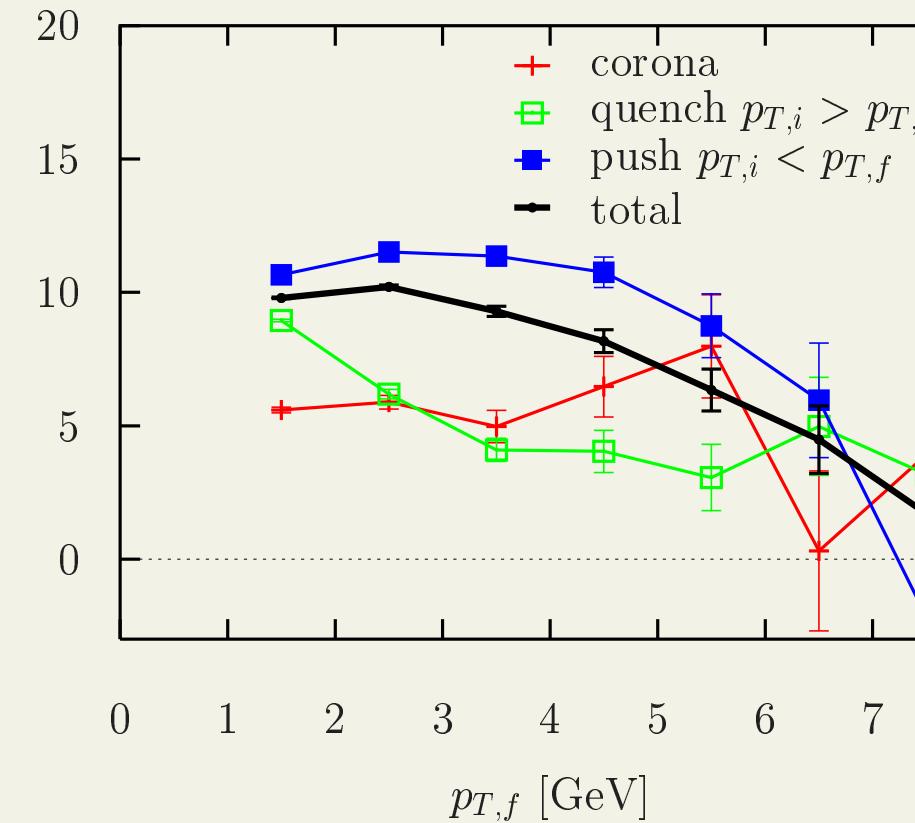
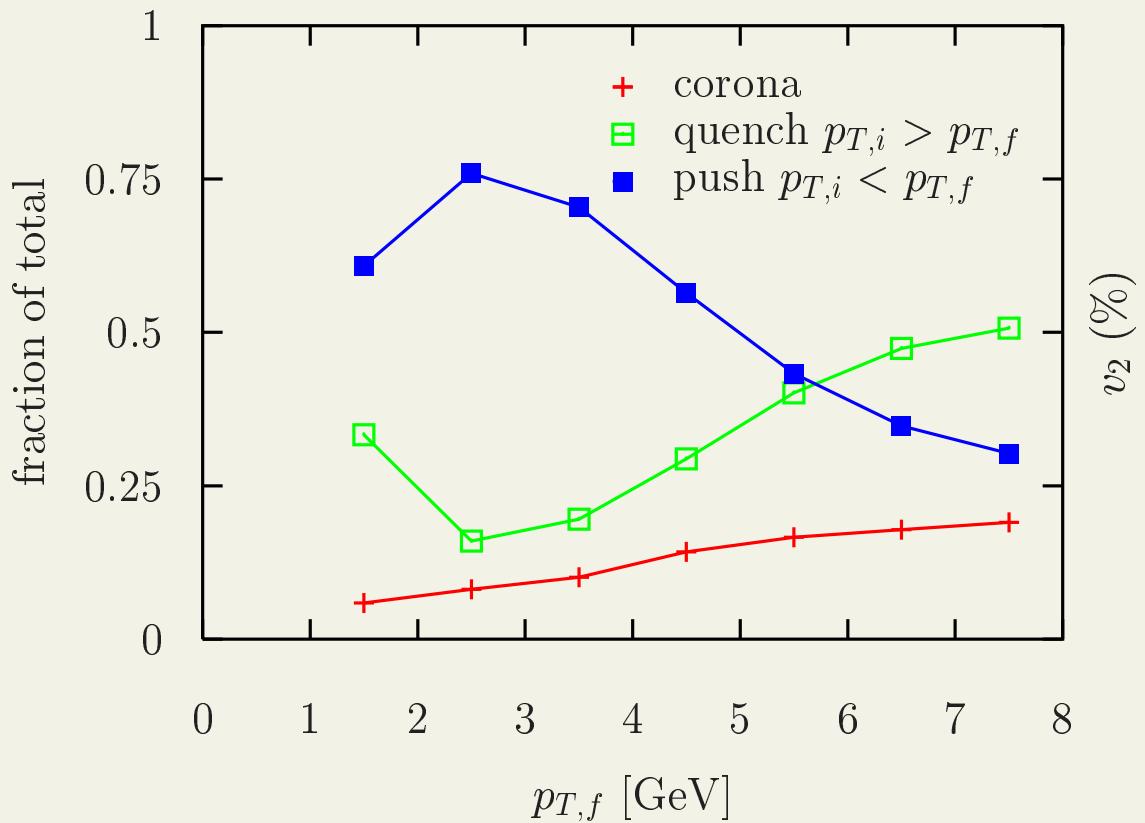
Though initial fluctuations NOT small perturbations, jet and medium $v_{2,3,4}$ correlate well with initial $\vec{\epsilon}_{2,3,4}$. For basic observables averaging even appears to nearly commute with evolution. (Where is the nonlinearity??)

We also find that, with GLV energy loss, transverse expansion reduces both R_{AA} and v_2 at high p_T .

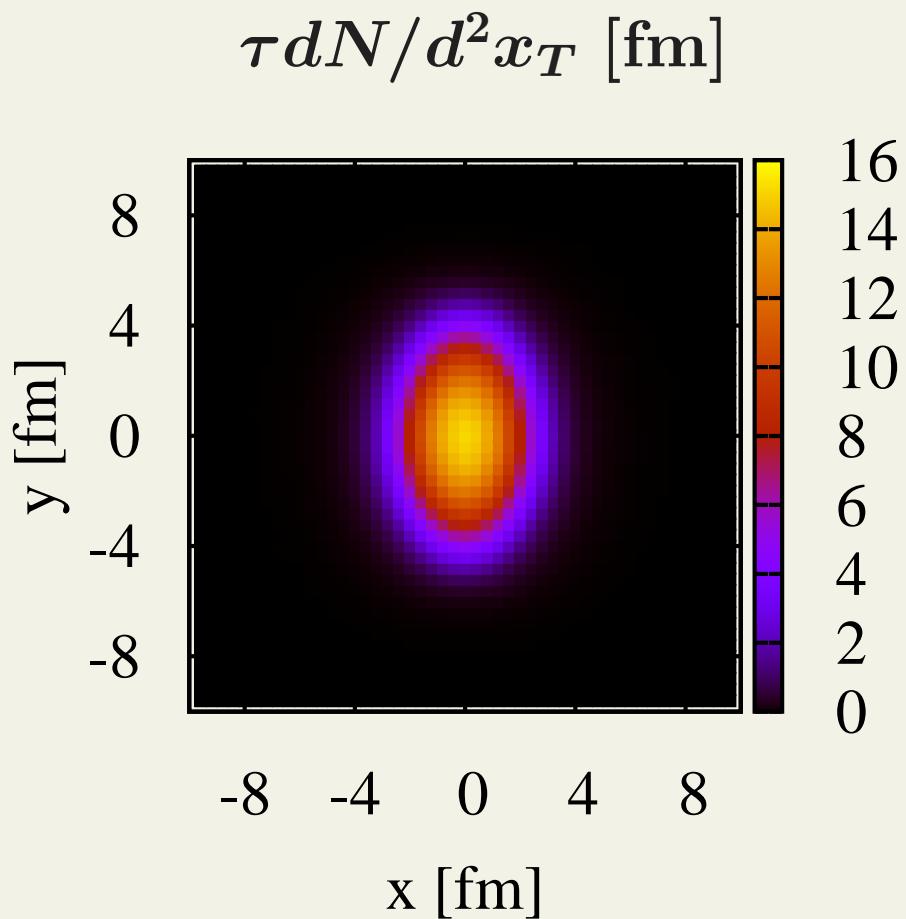
Some interesting avenues to investigate:

- dynamical fluctuations in transport
- migration in p_T (“plasma push” DM nucl-th/0503051)
- corona

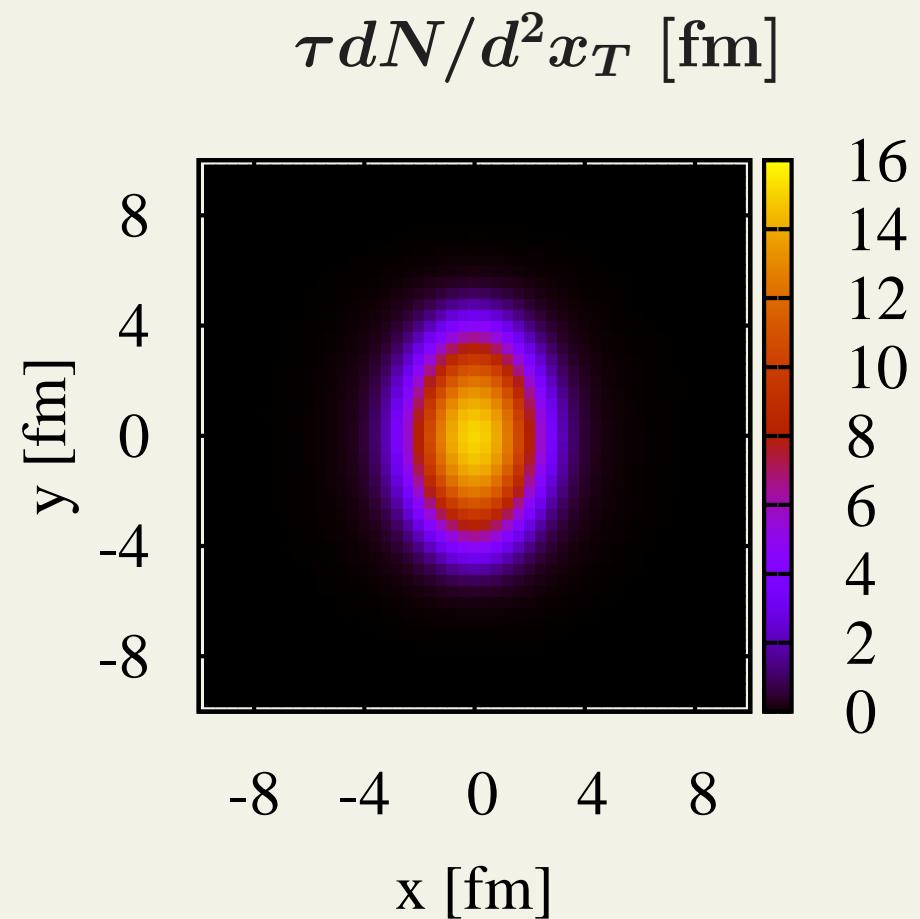
DM ('05):



average Au+Au, b=8 fm

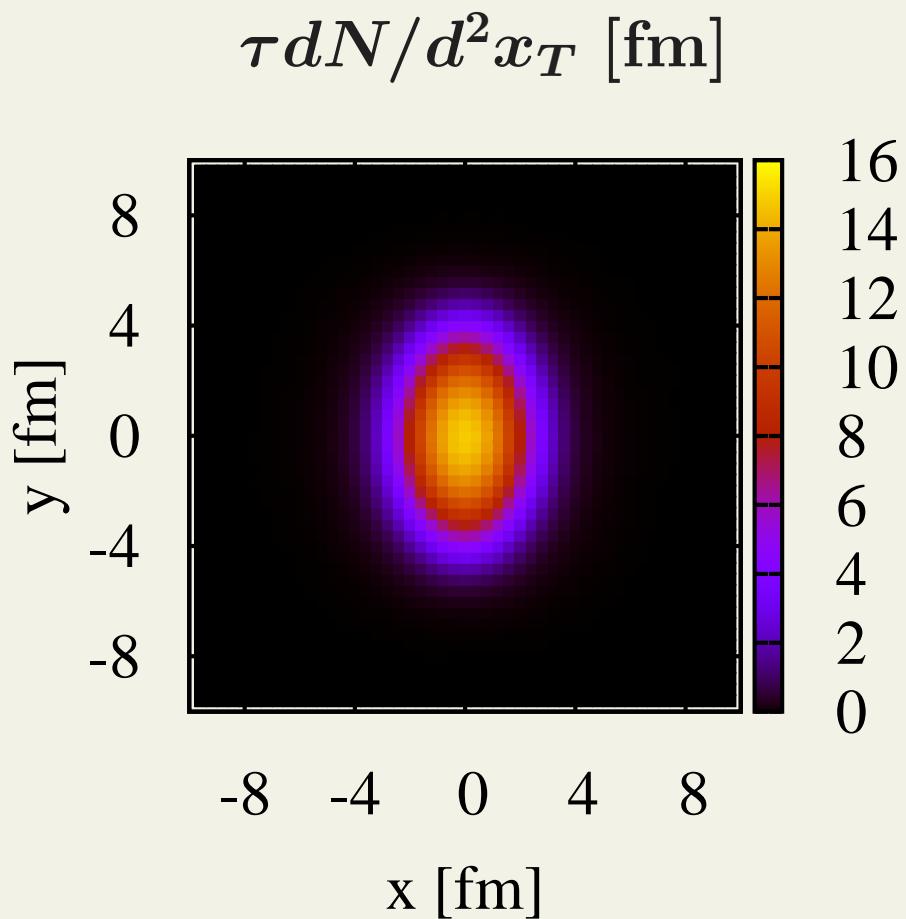


600 averaged MC Glauber runs

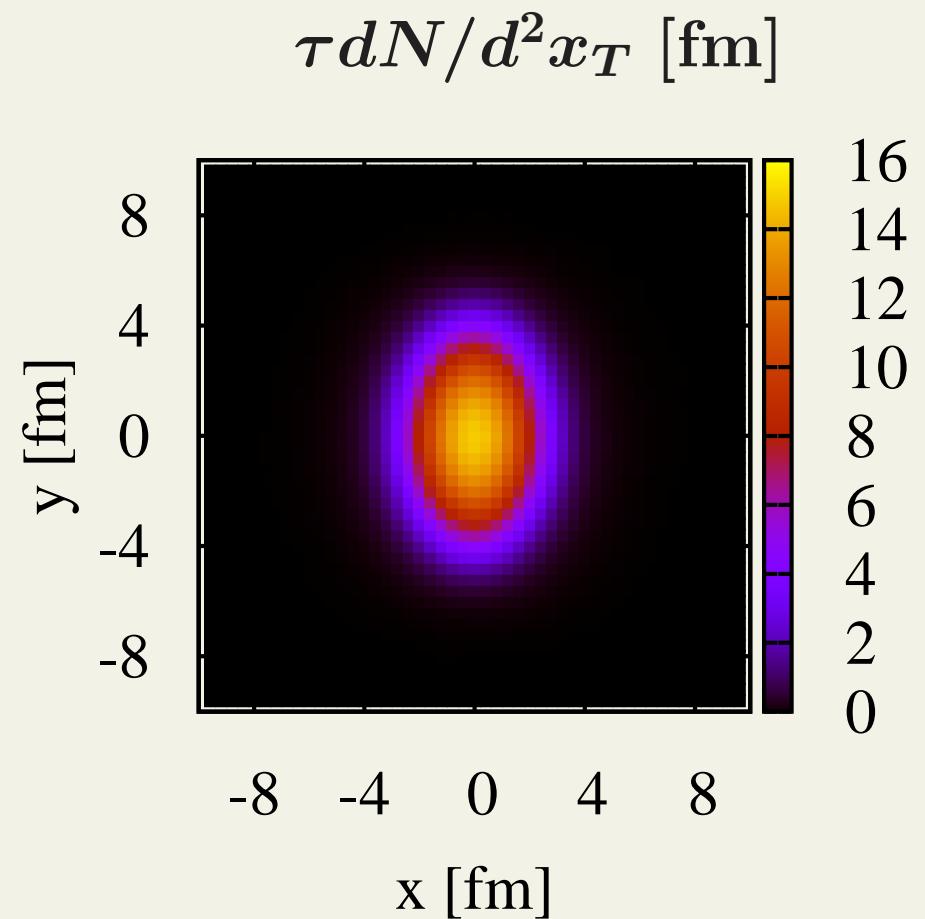


$\tau = 0.6$ fm

average Au+Au, b=8 fm

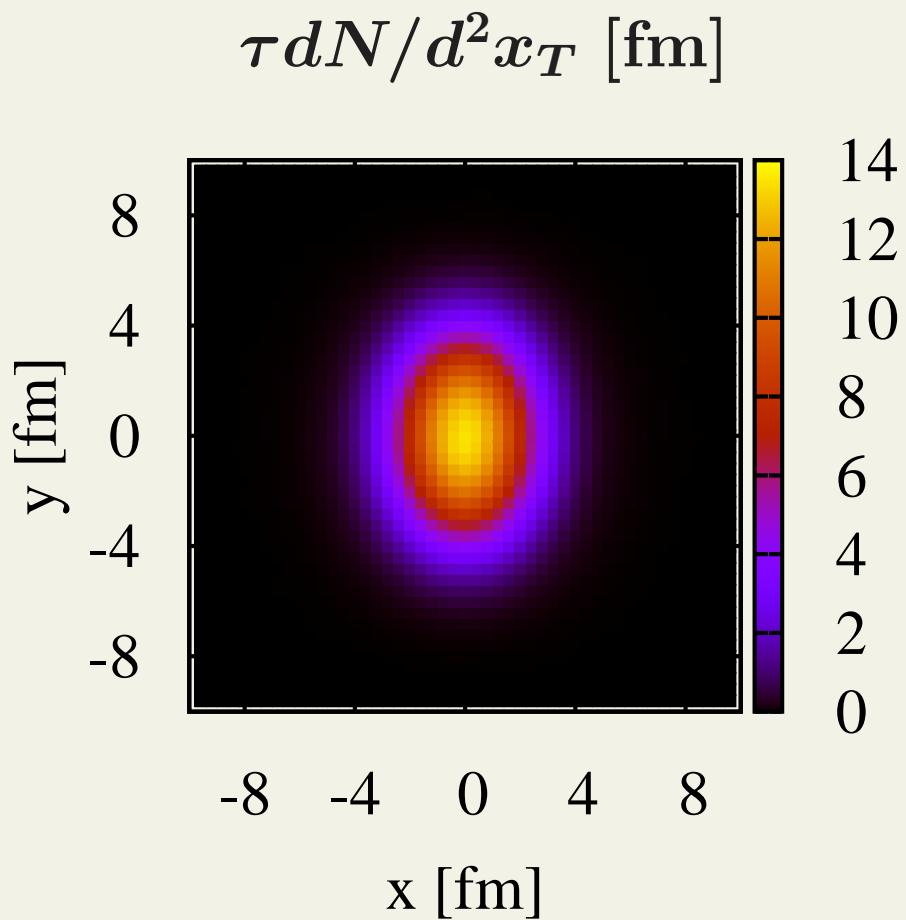


600 averaged MC Glauber

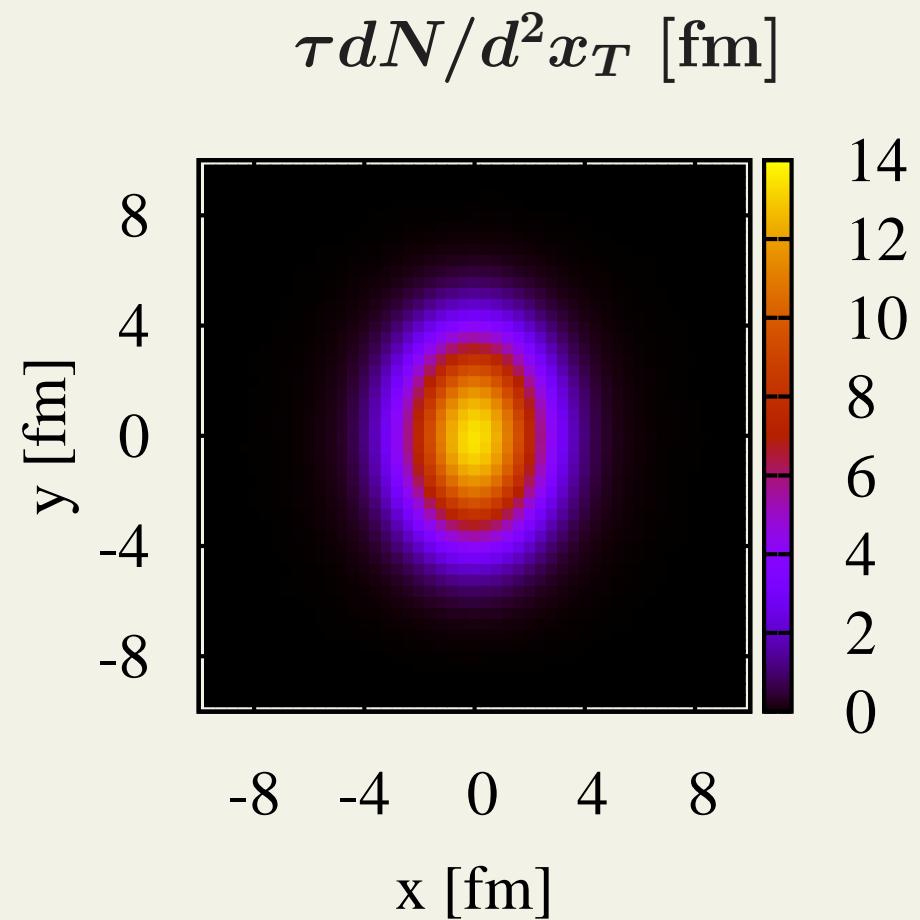


$\tau = 1.2$ fm

average Au+Au, b=8 fm

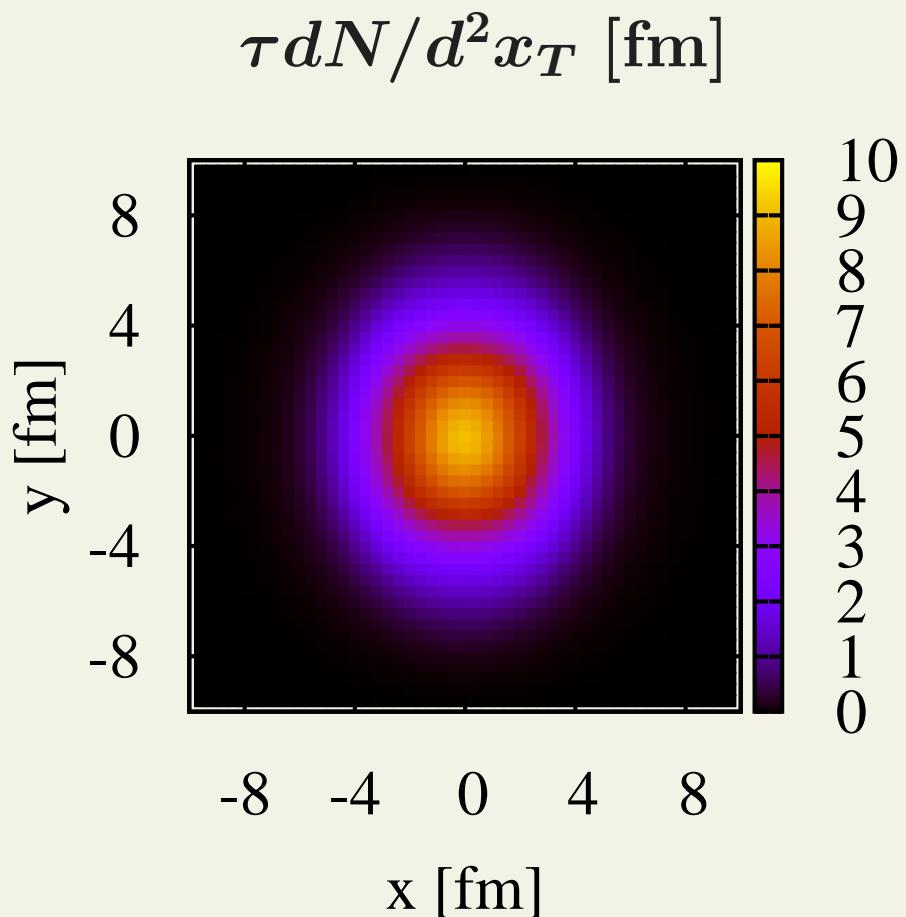


600 averaged MC Glauber

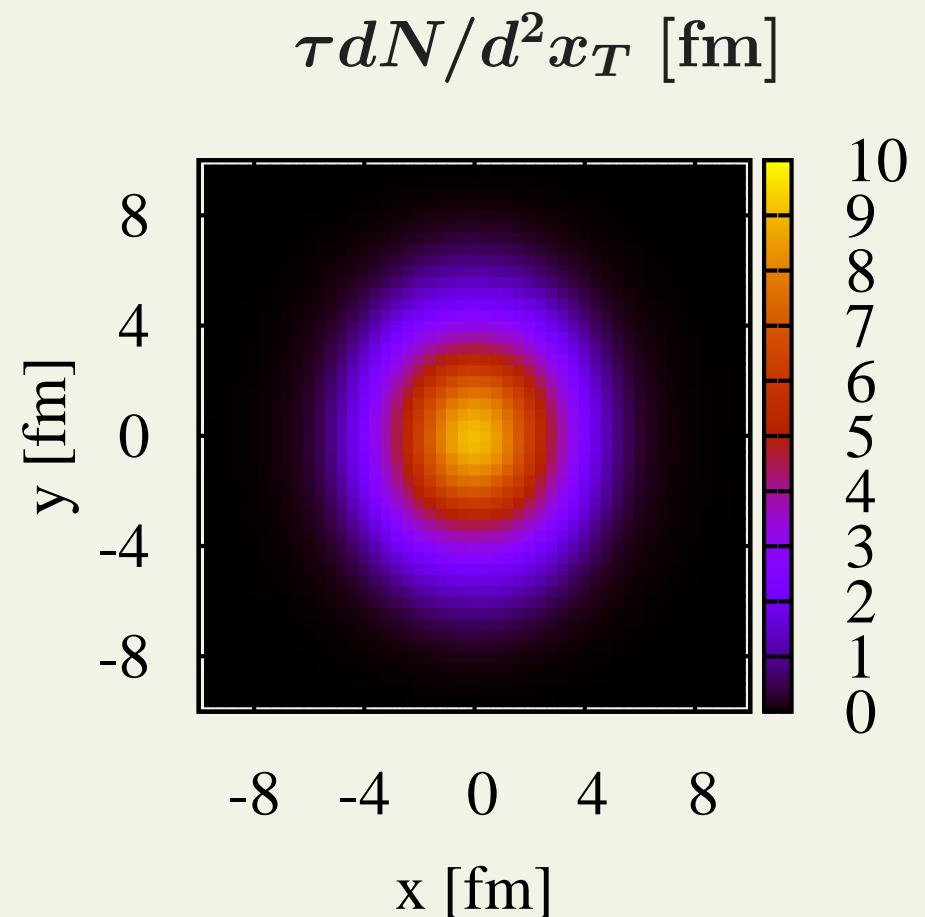


$$\tau = 2.1 \text{ fm}$$

average Au+Au, b=8 fm



600 averaged MC Glauber

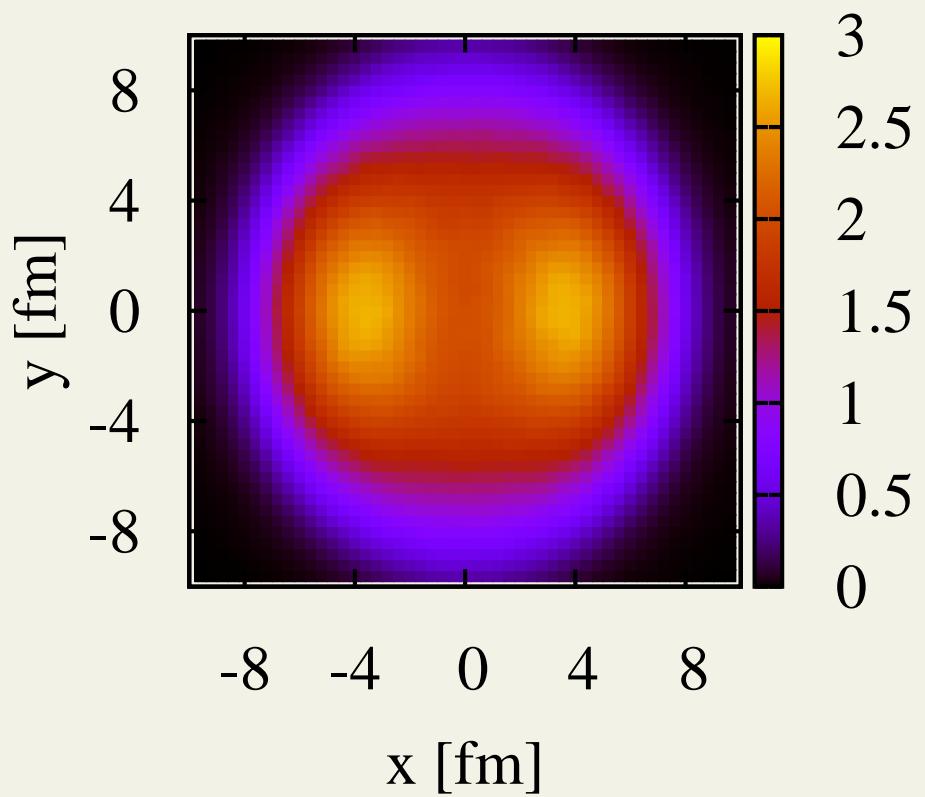


$$\tau = 3.6 \text{ fm}$$

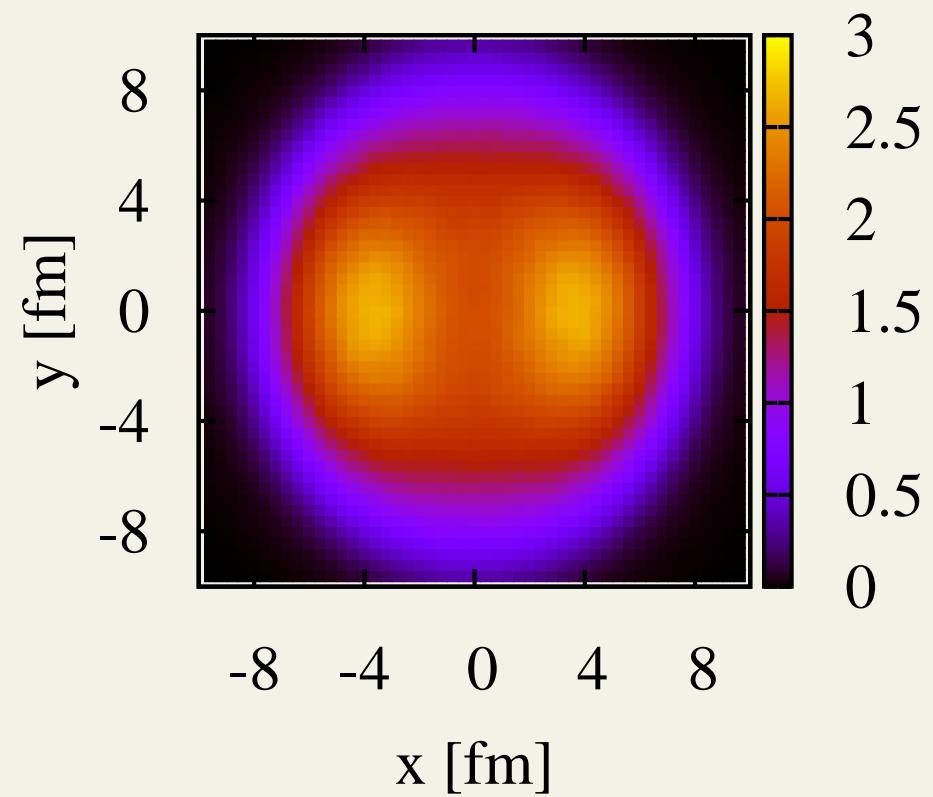
average Au+Au, b=8 fm

600 averaged MC Glauber

$$\tau dN/d^2x_T \text{ [fm]}$$

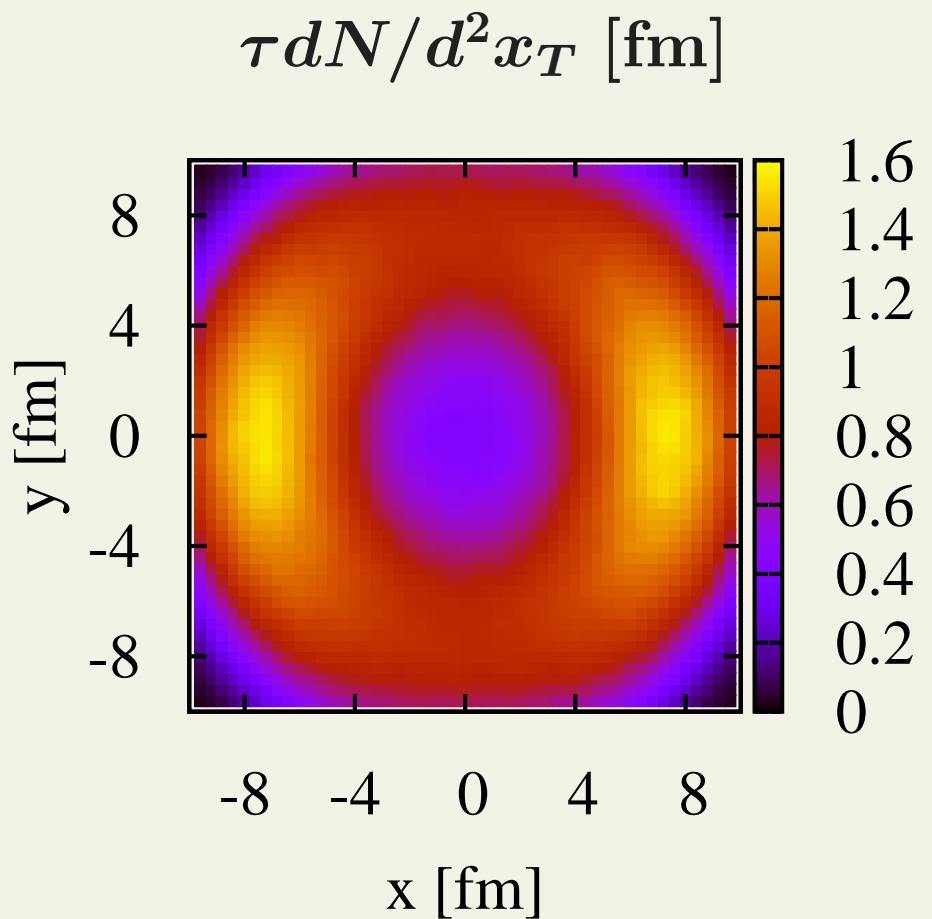


$$\tau dN/d^2x_T \text{ [fm]}$$

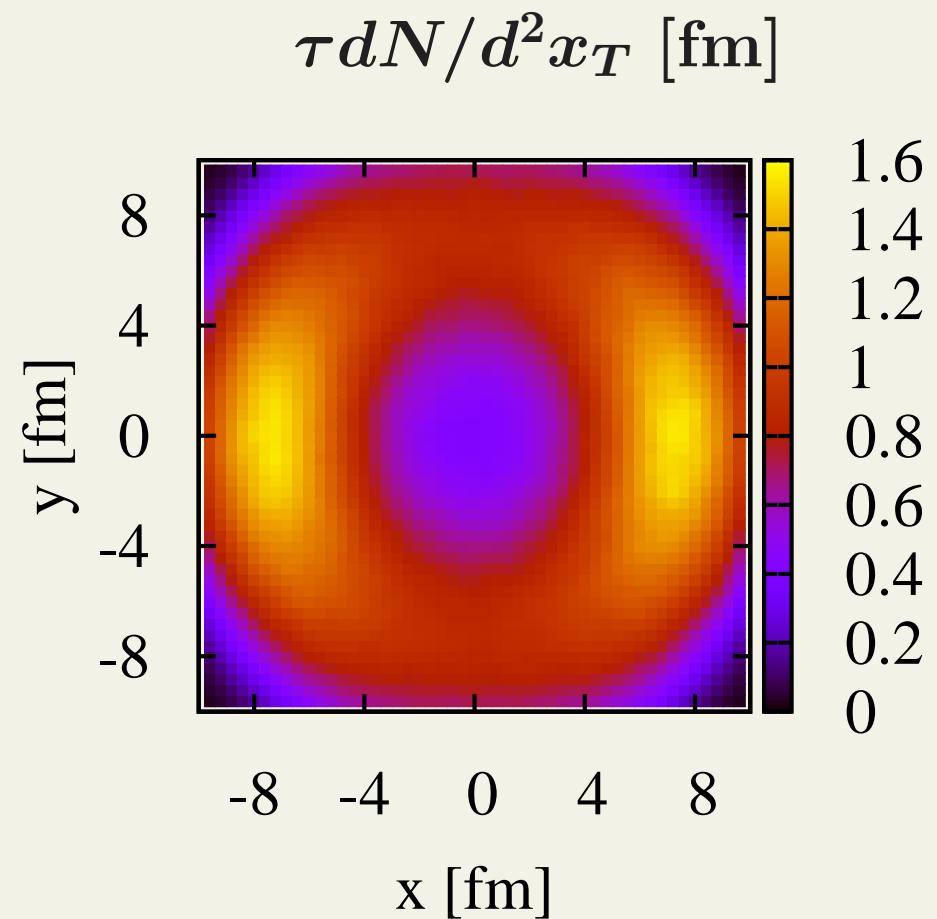


$$\tau = 6.6 \text{ fm}$$

average Au+Au, b=8 fm



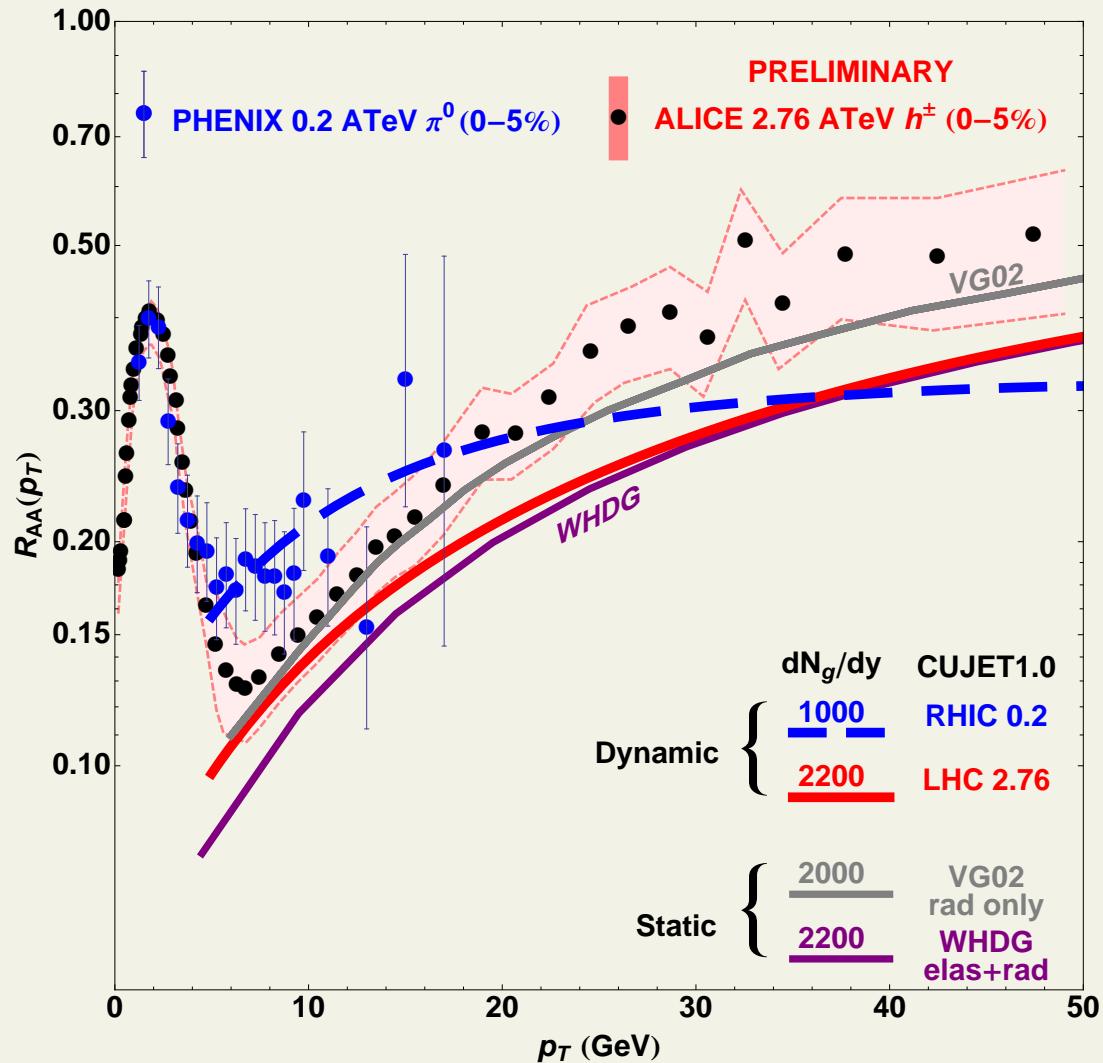
600 averaged MC Glauber



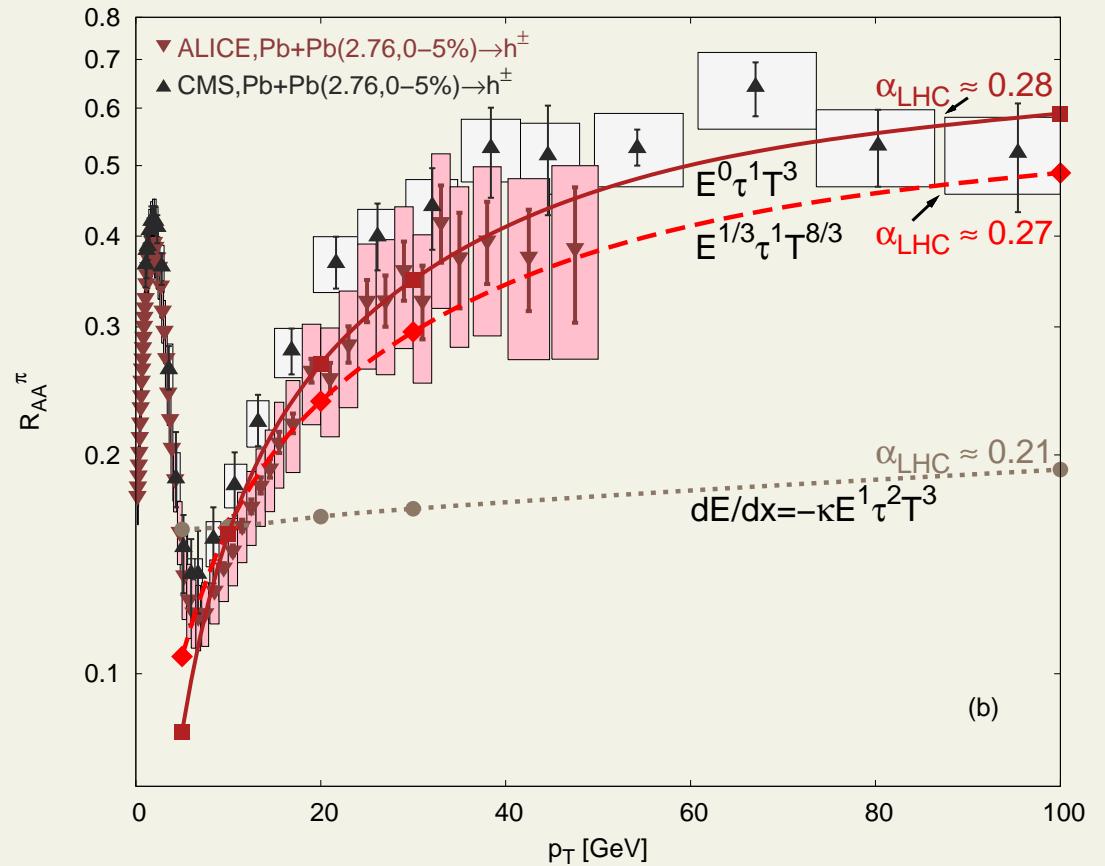
$$\tau = 9.6 \text{ fm}$$

Backup slides

CUJET 1.0 Buzzatti et al ('11)

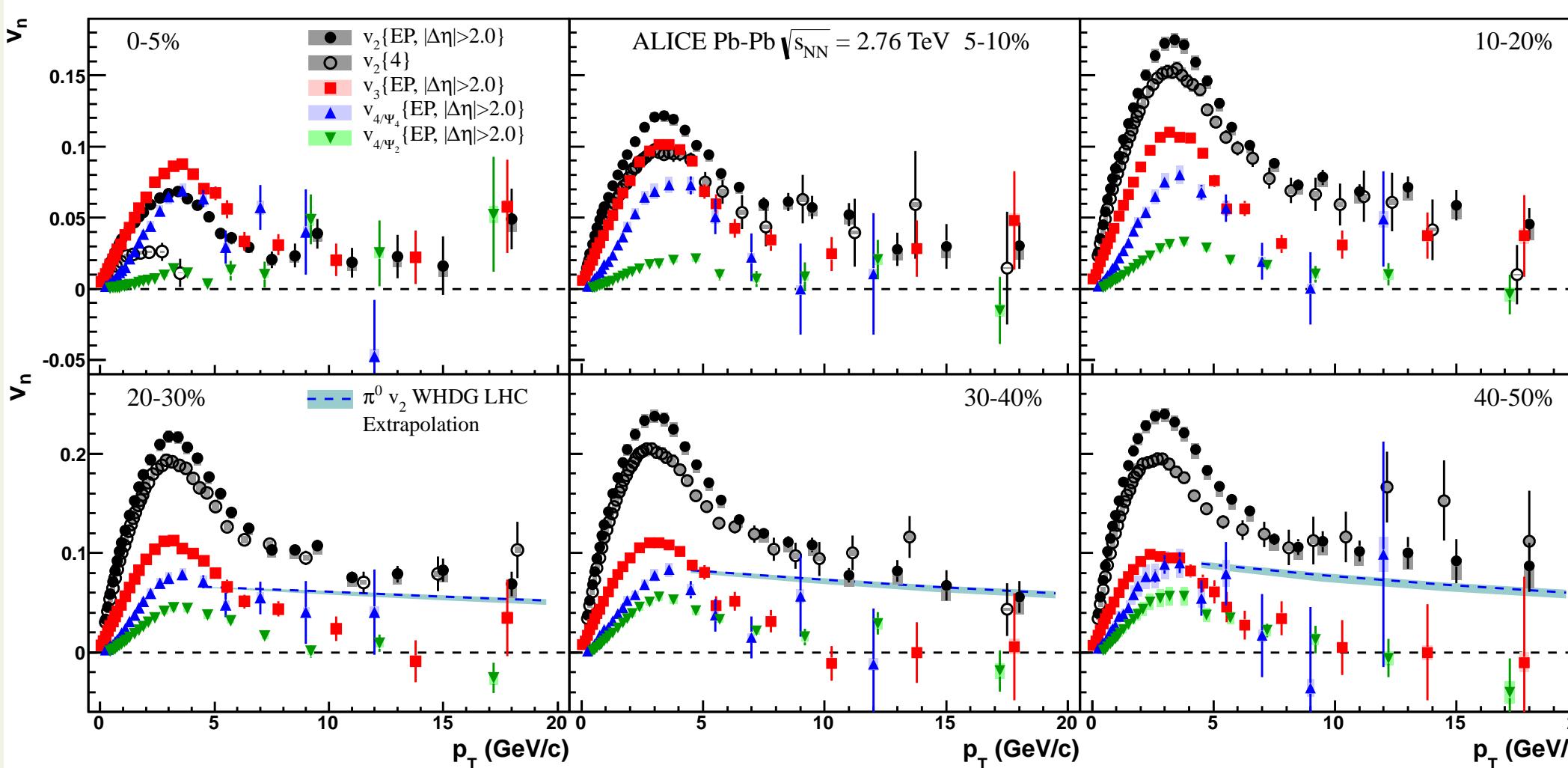


Betz & Gyulassy, arXiv:1201.0281

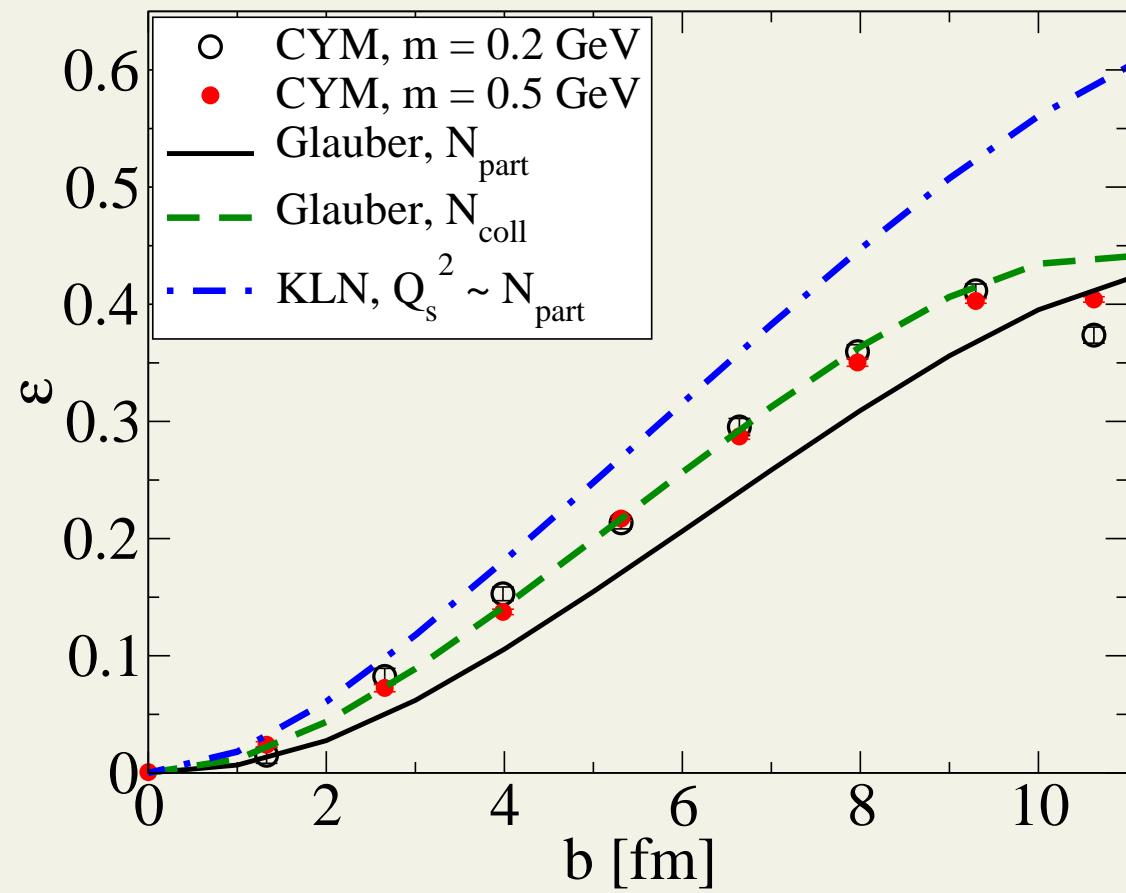


$$\alpha_s^{RHIC} = 0.3$$

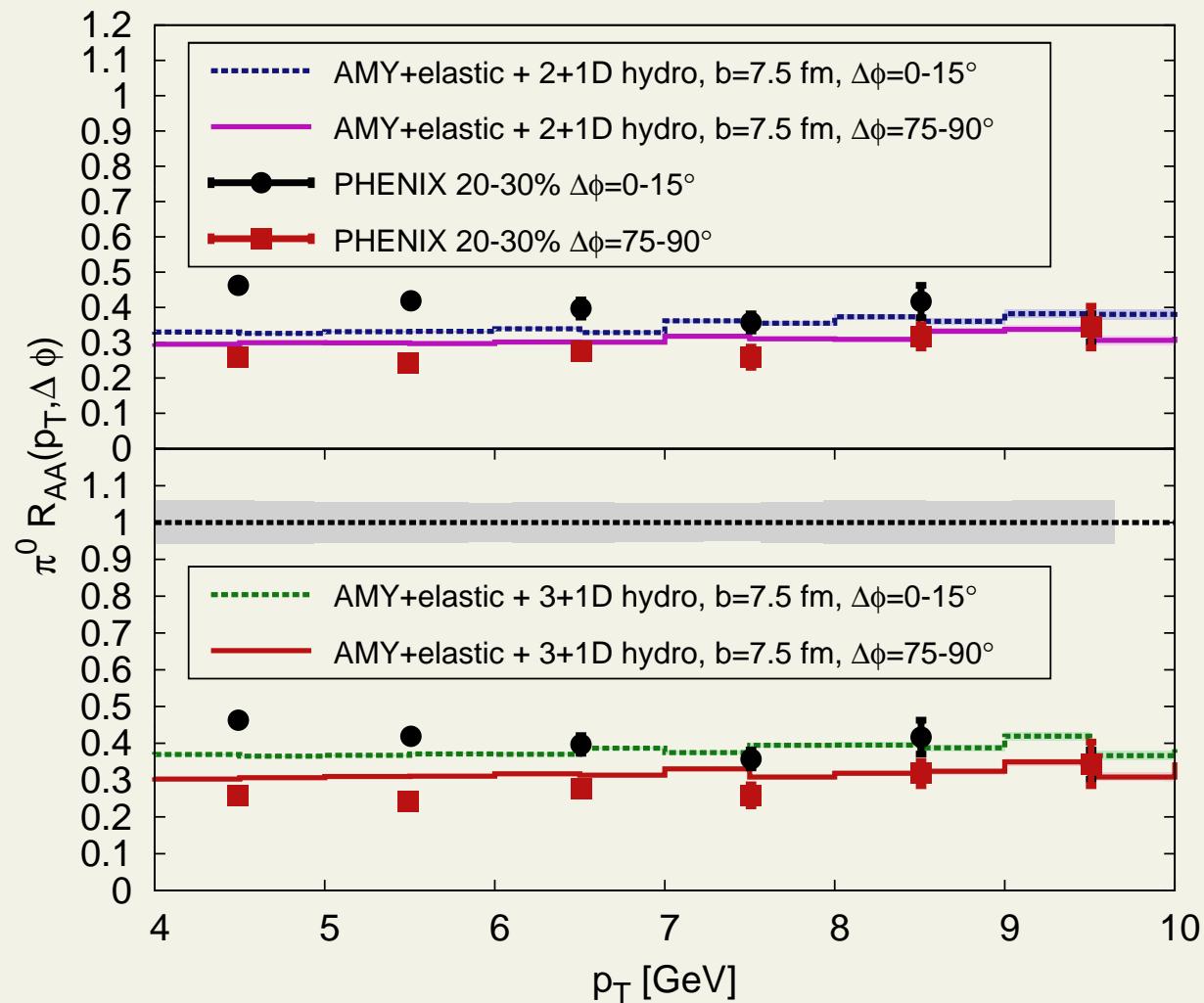
ALICE v2,v3,v4 arXiv:1205.5761v2



CYM eccentricity Venugopalan & Lappi, PRC74 ('06):

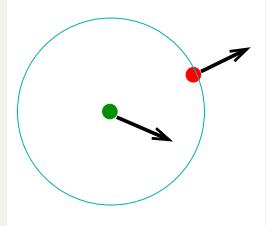


MARTINI $R_{AA}(\phi)$ Schenke et al, PRC80 ('09):



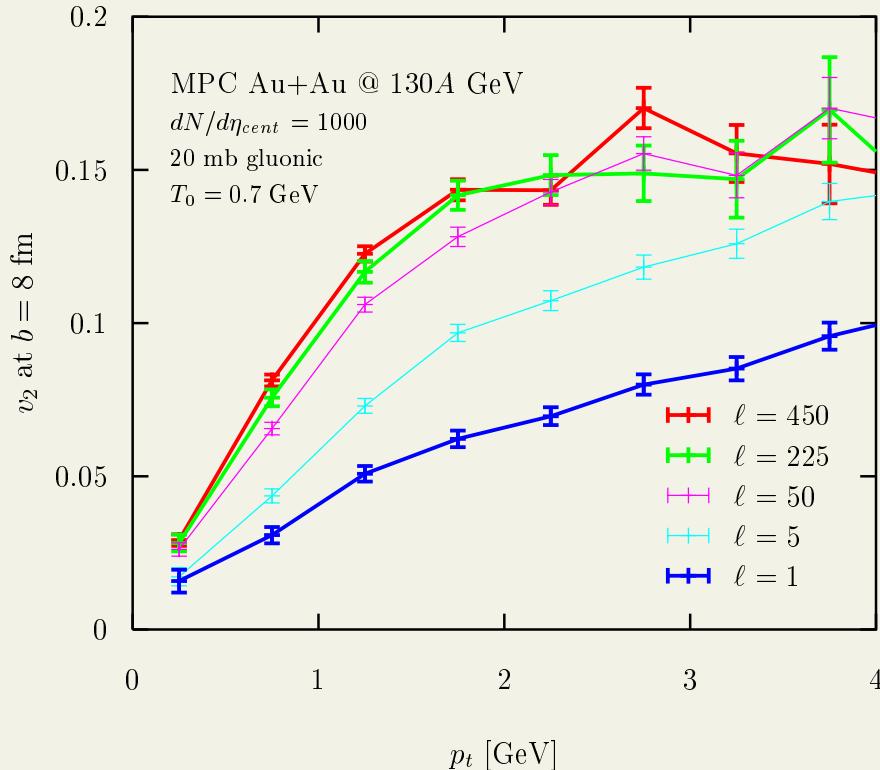
Parton subdivision

Naive $2 \rightarrow 2$ cascade nonlocal - action at distance $d < \sqrt{\frac{\sigma}{\pi}}$

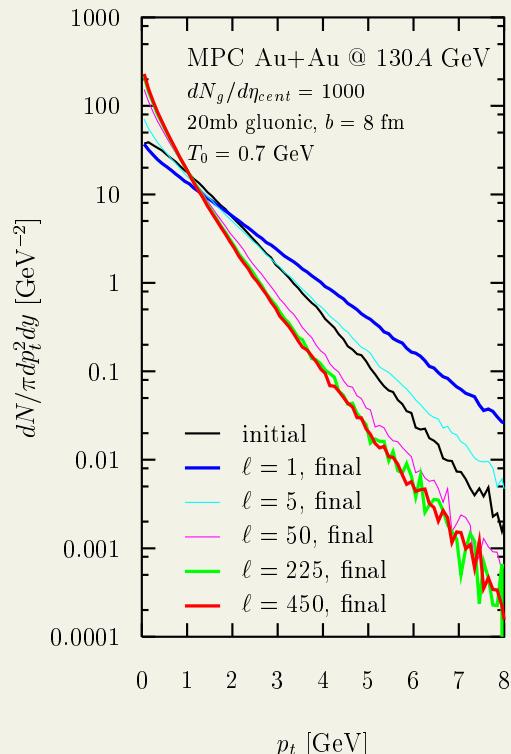


subdivision: rescale $f \rightarrow f \cdot \ell$, $\sigma \rightarrow \sigma/\ell$ $\Rightarrow d \propto \ell^{-1/2}$ local as $\ell \rightarrow \infty$

DM & Gyulassy ('02): $v_2(p_T)$



spectra



at RHIC: need subdivision $\ell \sim 200$ to eliminate large artifacts

→ computational challenge - CPU time scales as $\ell \sim 3/2$ per run → barely fits on PC